Research on two dimensional Wiener stochastic degradation model based on the wear model

Hui Zhang\textsuperscript{a}, Jun Yao and Yan-Lin Zhao

School of Reliability and System Engineering, Beijing University of Aeronautics and Astronautics, Beijing, China

Abstract. One dimensional Wiener degradation process is often used to describe the degradation of product performance. However one dimensional Wiener degradation process doesn’t sufficiently consider the relevance of multiple degradation factors and wear process, which lead to inaccurate results. To overcome these problems, a new two dimensional Wiener stochastic degradation model is proposed, which applies to the products on wear process and stochastic degradation process. Combining wear model and two dimensional Wiener stochastic degradation model, a new reliability analytical form is obtained by constructing the Fokker-Planck equation. Then using the relation among wear volume, degradation characteristic lifetime and drift parameter, parameters of two dimensional Wiener degradation model on the basic of wear model can be estimated. Compared with the existing approaches, the proposed method can effectively improve accuracy. Finally, a case study is illustrated the application and advantages of the proposed method.

1 Introduction

Products subjected to the action of the external environment, the material properties of the product will gradually change. And because of the randomness of the external environment and the material properties, the degradation of the product is also random. So stochastic process\cite{1} is usually used to describe the degradation process of product performance. Wiener process\cite{2-5} is the most often used method to describe the degradation of product performance. Tang\cite{6} et al estimated failure time distribution by a Wiener degradation model based on intermediate data. Wang\cite{7} used degradation data of Wiener processes with random effects to study reliability level of the bridge. Peng\cite{8} et al proposed Bayesian method to assess the reliability of the products with Wiener process degradation. Nicolai\cite{9} et al proposed an application to coatings on steel structures by comparing models for measurable deterioration with Wiener processes. Balka\cite{10} et al reviewed and implemented the cure models based on first hitting times of Wiener processes. Si\cite{11} et al estimated remaining useful life based on a nonlinear diffusion degradation process with monitoring degraded signal. Most of the studies on degradation of product performance are based on one dimensional Wiener process degradation, without taking into account the multiple degradation and the physical mechanism of degradation.

Wear is one of the common failure types of components. When the wear occurs, the features of the product can be reduced or failed, reliability and safety will be lost if products are continued to put into
use. Many scholars have put forward relevant theories and models about the wear[12,13], which predict the lifetime of the products by calculating the wear volume and wear rate. Hu[14] et al proposed finite element modeling (FEM) approaches with Lagrangian increment method for 3D metal turning of hardened steel H13 by common ceramic tool and ultrafine-grained tool respectively have been investigated by simulation of DEFORM-3D software and turning test. Lin[15] combined the finite element numerical simulation analysis method with the Archard wear calculation model and temperature effect, predicted the most serious wear parts, and proposed a formula for calculating the total wear rate. Gao[16] et al estimated die service life of forging spiral gear based on modified Archard method. Kim[17] et al estimated die service life against plastic deformation and wear during hot forging processes with finite element modeling. Most researches on the wear only consider physical mechanism of wear, predict wear rate and the wear volume by finite element simulation, without considering the impact of the external environment randomness on products degradation.

In this paper, on the basis of the wear model, considering the influence of the randomness of the external environment on the products degradation, combined with the theory of random degradation, a model of two dimensional Wiener stochastic degradation model is proposed based on the wear model. Using 1000h reliability test data of the steam turbine pump as an example, the rationality and accuracy of the method proposed in this paper is verified by comparing with calculation results of other methods.

2 The performance degradation model based on two dimensional Wiener process

2.1 Binary linear Wiener process model

Assuming that product performance degradation process in \( \{X(t) = (X_1(t), X_2(t))^T, t \geq 0\} \) [18], namely, the degradations of products are binary. At the time \( t \), it follows:

\[
X(t) \sim N(t \mu, t \Sigma)
\]

where

\[
\mu = (\mu_1, \mu_2)^T, \Sigma = \begin{pmatrix}
\sigma_1^2 & \rho \sigma_1 \sigma_2 \\
\rho \sigma_1 \sigma_2 & \sigma_2^2
\end{pmatrix}
\]

\( \rho \) is the correlation coefficient. Assume \( \rho \neq 0 \), which means the two marginal degradation process \( \{X_1(t), t \geq 0\} \) and \( \{X_2(t), t \geq 0\} \) are related.

2.2 Reliability Assessment

Initial degradation \( X_1(t) = X_2(t) = 0 \), When one of \( \{X_1(t), t \geq 0\} \) and \( \{X_2(t), t \geq 0\} \) exceeds its failure threshold, product fails. The lifetime of the product can be represented as:

\[
T = \inf\{t : X_1(t) > l_1 \text{ or } X_2(t) > l_2\}
\]

Then the reliability function \( R(t) \) is derived:

\[
R(t) = P\{X_1(s) < l_1, X_2(s) < l_2, 0 \leq s \leq t\}
\]

When Domine and Pieper[19] studied the first hitting time of binary Wiener process, the Fokker-Planck equation was constructed (Kolmogrov forward equation) based on the initial performance
of $X_1(0) = x_{0,1}$ and $X_2(0) = x_{0,2}$, the analytic form of the reliability function $R(t)$ was obtained by solving the equation:

$$R(t) = \int_0^\infty \sum_{n=1}^{\infty} \frac{2r}{\alpha \sigma_n^2 (1 - \rho^2) t} \sin\left(\frac{n\pi}{\alpha} \varphi_0\right) \exp\left[\frac{\sigma_n^2 \mu_t - \sigma_t^2 \rho \cos \varphi - \frac{\mu_t^2}{\sigma_n^2 (1 - \rho^2)} \sigma_n^2 \sin \varphi}{\sigma_n^2 \sqrt{1 - \rho^2}}\right] \exp\left[\frac{(\mu_1 \rho \sigma_1 - \mu_2 \sigma_2^2) x_{0,2} + (\mu_2 \rho \sigma_2 - \mu_1 \sigma_2^2) x_{0,1}}{(1 - \rho^2) \sigma_1^2 \sigma_2^2}\right] \exp\left[\frac{-\sigma_1^2 \mu_1^2 - 2\mu_2 \sigma_1 \sigma_2^2 \rho + \sigma_2^2 \mu_2^2}{2(1 - \rho^2) \sigma_1^2 \sigma_2^2} t - \frac{r_r^2 + r_0^2}{2(1 - \rho^2) \sigma_1^2 \sigma_2^2} \right] \sin\left(\frac{n\pi}{\alpha} \right) I_v\left(\frac{rr_0}{(1 - \rho^2) \sigma_1 \sigma_2 t}\right) dr d\varphi$$

Where $\alpha = \arctan\left(-\frac{\sqrt{1 - \rho^2}}{\rho}\right) + \pi$; $r_0$, $\varphi_0$ are the solution of the equation below:

$$\begin{align*}
r_0 \cos \varphi_0 &= \frac{\sigma_2}{\sigma_1} (l_1 - x_{0,1}) - \rho (l_2 - x_{0,2}) \\
r_0 \sin \varphi_0 &= \sqrt{1 - \rho^2} (l_2 - x_{0,2})
\end{align*}$$

$I_v(z)$ is the modified Bessel function.

$$I_v(z) = \sum_{k=0}^{\infty} \frac{\left(\frac{z}{2}\right)^{2k+v}}{k! \Gamma(k + v + 1)}$$

When $x_{0,1} = x_{0,2} = 0$, the reliability function $R(t)$, lifetime function $F(t) = 1 - R(t)$, and density function $f(t) = dF(t) / dt = -dR(t) / dt$ will be obtained. If $x_{0,1}$ and $x_{0,2}$ in formula (5) are regarded as the performance degradation when product run to a certain time, then formula (5) is actually the reliability of the continue running time of product, and $F(t) = 1 - R(t)$ is the distribution of the remaining lifetime.

### 2.3 The performance degradation data model

Assuming a total of N products of a degradation test, at the time of $t_{i_1}, t_{i_2}, \cdots, t_{i_m}$, measure the degradation X and Y and get measured data:

$$\begin{align*}
X_{11}, X_{12}, \cdots, X_{1m_1} & \quad Y_{11}, Y_{12}, \cdots, Y_{1m_1} \\
X_{21}, X_{22}, \cdots, X_{2m_2} & \quad Y_{21}, Y_{22}, \cdots, Y_{2m_2} \\
\vdots & \quad \vdots \\
X_{n1}, X_{n2}, \cdots, X_{nm_n} & \quad Y_{n1}, Y_{n2}, \cdots, Y_{nm_n}
\end{align*}$$

(8)
Note $\Delta X_y = X_y - X_{i,j-1}, \Delta Y_y = Y_y - Y_{i,j-1}, i = 1,2,\cdots, n, j = 1,2,\cdots m_i$ as the degradation increment of sample $i$ during moment $t_{i,j-1}$ to $t_{i,j}$, thus the following data is derived:

$$
\begin{align*}
\Delta X_{11}, & \Delta X_{12}, \cdots \Delta X_{1m_i}, \Delta Y_{11}, \Delta Y_{12}, \cdots \Delta Y_{1m_i} \\
\Delta X_{21}, & \Delta X_{22}, \cdots \Delta X_{2m_i}, \Delta Y_{21}, \Delta Y_{22}, \cdots \Delta Y_{2m_i} \\
\vdots & \vdots \vdots \cdots \vdots \vdots \vdots \\
\Delta X_{n1}, & \Delta X_{n2}, \cdots \Delta X_{nm_i}, \Delta Y_{n1}, \Delta Y_{n2}, \cdots \Delta Y_{nm_i}
\end{align*}
$$

(9)

3 Method for estimating parameter $\mu$ and $\sigma^2$

3.1 Maximum likelihood estimation

$\Delta X_y, \Delta Y_y$ are degradation increment of sample $i$ from $t_{i,j-1}$ to $t_{i,j}$, note $\Delta t_y = t_y - t_{i,j-1}$, $(\Delta X_y, \Delta Y_y)^T$ are independent and obey two-dimensional normal distribution $N(\mu\Delta t_y, \Sigma)$. Using the maximum likelihood estimation (MLE) method to get the estimated values of $\mu_1, \sigma_1^2, \mu_2, \sigma_2^2$:

$$
\hat{\mu}_i = \frac{\sum_{i=1}^{n} X_{in_i}}{\sum_{i=1}^{n} t_{in_i}} \quad \text{and} \quad \sigma_i^2 = \frac{1}{\sum_{i=1}^{n} m_i} \left[ \sum_{i=1}^{n} \sum_{j=1}^{m_i} \left( \frac{(\Delta X_y)^2}{\Delta t_y} - \frac{\left( \sum_{i=1}^{n} X_{in_i} \right)^2}{\sum_{i=1}^{n} t_{in_i}} \right) \right] \tag{10}
$$

$$
\hat{\mu}_2 = \frac{\sum_{i=1}^{n} Y_{in_i}}{\sum_{i=1}^{n} t_{in_i}} \quad \text{and} \quad \sigma_2^2 = \frac{1}{\sum_{i=1}^{n} m_i} \left[ \sum_{i=1}^{n} \sum_{j=1}^{m_i} \left( \frac{(\Delta Y_y)^2}{\Delta t_y} - \frac{\left( \sum_{i=1}^{n} Y_{in_i} \right)^2}{\sum_{i=1}^{n} t_{in_i}} \right) \right] \tag{11}
$$

Estimation of the correlation coefficient:

$$
\hat{\rho} = \frac{1}{M\hat{\sigma}_1\hat{\sigma}_2} \left[ \frac{\sum_{i=1}^{n} \sum_{j=1}^{m_i} (\Delta X_y - \hat{\mu}_1\Delta t_y)(\Delta Y_y - \hat{\mu}_2\Delta t_y)}{\Delta t_y} \right] \tag{12}
$$

In this paper, in order to measure the two degradations at the same time, the equal interval measurement is adopted, which is so called stable measurement, i.e. $\Delta t_y = \Delta t$, so $(\Delta X_y, \Delta Y_y)^T$ are independent and identically distributed bivariate normal samples,

$$
(\Delta X_y, \Delta Y_y)^T \sim N(\mu\Delta t, \Sigma \Delta t) \tag{13}
$$

the estimations of $\mu_1, \sigma_1^2, \mu_2, \sigma_2^2$ by the properties of the multivariate normal distribution is derived as follows:
3.1 Maximum likelihood estimation

Method for estimating parameter sample $i$ during moment derived as follows:

Estimation of the correlation coefficient:

Using the maximum likelihood estimation (MLE) method to get the estimated value $s$ of $X_{ij}$, note

Estimation of the correlation coefficient:

\[
\hat{\rho} = \frac{1}{\Delta t \hat{\sigma}_1 \hat{\sigma}_2} \sum_{i=1}^{n} \sum_{j=1}^{m} (\Delta X_{ij} - \hat{\mu}_1 \Delta t)(\Delta Y_{ij} - \hat{\mu}_2 \Delta t)
\]

3.2 Parameter estimation of two dimensional Wiener stochastic degradation model based on the wear model

3.2.1 Archard Wear Model

The Archard wear model is a classic wear calculation model by Professor J.F. Archard[20]. The model is verified by experiment and it has a good practicability. The model is as follows:

\[
\alpha = \frac{F_n S}{H} \propto a + b \gamma
\]

Where $V$ and $S$ are the wear volume and relative slip distance, respectively, $F_n$ is the normal force, $K$ is the wear coefficient, $H$ is the Brinell hardness. Whereas $a$ and $b$ are unknown parameters, $\gamma$ is a variable.

Archard[21] wear model is a linear model, it can be seen that wear volume is a linear function of time $t$, considering the randomness in the process of wear, the Archard wear model is combine with the Markov model to form a new wear model:

\[
\Delta \propto \alpha_0 + \alpha_1 t + \epsilon
\]

Where $\Delta$ is the wear volume, $\alpha_0$ and $\alpha_1$ are determined coefficient, $\epsilon$ is a random diffusion, and $\epsilon \sim N(0, \sigma^2)$, $t$ is the characteristic lifetime.

We use $T$ to represent the lifetime of the product, so its expectation is $E(T) = \frac{1}{\alpha_1} \frac{\alpha_0 - \epsilon}{\epsilon}$. By measuring the degradation of products at $T_1, T_2, \cdots T_n$, $X_1, X_2, \cdots X_n$ are obtained. So the point estimations of $\alpha_0, \alpha_1$ are:

\[
\hat{\alpha}_0 = \bar{X} - \frac{\bar{X} \sum (T_i - \bar{T})(X_i - \bar{X})}{\sum (T_i - \bar{T})^2}, \hat{\alpha}_1 = \frac{\bar{X} \sum (T_i - \bar{T})(X_i - \bar{X})}{\sum (T_i - \bar{T})^2}
\]
3.2.2 Method of parameter estimation of two dimensional Wiener degradation model based on the wear model

In the Wiener process, the distribution of product lifetime $T$ is inverse Gaussian distribution, and the characteristic function of $T$ can be calculated because of the stability of Wiener process and the characteristic of independent increment, which is $E[\exp(-\theta T)] = \exp\left\{-\frac{l \left(\sqrt{\mu_2 + 2\theta} - \mu_1\right)}{\mu_1}\right\}$, and its expectation is: $E[T] = \frac{l}{\mu}$ . It can be seen that the expectation of lifetime $T$ is only related to the drift parameter. When one of the two degradations exceeds its failure threshold, product fails. In this case, the working time is the lifetime of the product. By combining the two expectations, it follows:

$$E(T_1) = \frac{l_1}{\mu_1} \approx \frac{l_1 - \alpha_{11} - \varepsilon}{\alpha_{12}} \quad E(T_2) = \frac{l_2}{\mu_2} \approx \frac{l_2 - \alpha_{21} - \varepsilon}{\alpha_{22}} \quad (20)$$

Estimations of $\mu_1, \mu_2$

$$\hat{\mu}_2 = \frac{l_2 \alpha_{22}}{l_2 - \alpha_{21} - \varepsilon}, \quad \hat{\mu}_2 = \frac{l_2 \alpha_{22}}{l_2 - \alpha_{21} - \varepsilon} \quad (21)$$

Bring them into the formula (21), the reliability function $R(t)$ and distribution function $F(t)$ of the model proposed in this paper are obtained:

$$R(t) = \int_0^\infty \frac{2r}{r^2 + \alpha^2} \sin\left(\frac{n\pi t}{\alpha}\right) \frac{l_2 \beta_{22}}{\sigma_i^2 \sqrt{1 - r^2} (l_i - \beta_{21} - \varepsilon)} r \cos \varphi \sin \varphi \, dr \, dt$$

$$F(t) = 1 - R(t) \quad (23)$$

4 The example of reliability assessment of steam turbine pump

Steam turbine is the power device of ship, and steam turbine pump is the key part of the steam turbine as the output device of lubricating oil. Once a fault occurs, it will affect the whole ship power system. Now a 1000h reliability test data of the steam turbine pump is used as an example to verify the rationality and accuracy of the method proposed in this paper. The 1000h reliability test of steam turbine pump can be divided into two stages. Firstly, individual diagnostic test for 60 hours. Then in the remaining 940 hours, according to the test pattern for continuous operation test, it is a total of 47 cycles with 20h for each cycle. Each cycle is interspersed with automatic variable conditions, parameter fluctuations, exhaust safety valve and other test items.

Steam turbine pump belongs to a complex mechanical system with continuous, variable condition, and reciprocating motion. Wear, fatigue and fracture of the parts are the main reasons for the lifetime and failure of the steam turbine pump. Therefore, both domestic and foreign researchers have proposed
characteristic of independent increment, which is characteristic function of $T$ can be calculated because of the stability of Wiener process and the In the Wiener process, the distribution of product lifetime $T$ is inverse Gaussian distribution, and the on the wear model

3.2.2 Method of parameter estimation of two dimensional Wiener degradation model based

model proposed in this paper are obtained:

4 The example of reliability assessment of steam turbine pump

rationality and accuracy of the method proposed in this paper. The 1000h reliability test of steam cycles with 20h for each cycle. Each cycle is interspersed with automatic variable conditions, the remaining 940 hours, according to the test pattern for continuous operation test, it is a total of 47 and failure of the steam turbine pump. Therefore, both domestic and foreign reseachers have proposed Bring them into the formula (21), the reliability function

Steam turbine pump belongs to a complex mechanical system with continuous, variable condition, and failure of the steam turbine pump. Therefore, both domestic and foreign reseachers have proposed

**Table 1.** Data of retarder rotor support bearing clearance and the support bearing temperature.

<table>
<thead>
<tr>
<th>Time (h)</th>
<th>100</th>
<th>200</th>
<th>300</th>
<th>400</th>
<th>500</th>
<th>600</th>
<th>700</th>
<th>800</th>
</tr>
</thead>
<tbody>
<tr>
<td>Support bearing temperature (℃)</td>
<td>62.81</td>
<td>63.64</td>
<td>61.67</td>
<td>63.45</td>
<td>61.41</td>
<td>59.89</td>
<td>63.08</td>
<td>63.77</td>
</tr>
<tr>
<td>Reducer rotor support bearing clearance (mm)</td>
<td>0.10</td>
<td>0.11</td>
<td>0.11</td>
<td>0.11</td>
<td>0.11</td>
<td>0.11</td>
<td>0.12</td>
<td>0.12</td>
</tr>
</tbody>
</table>

4.1 Reliability assessment of steam turbine pump

We use three methods to assess the reliability of steam turbine pump, respectively, one dimensional Wiener degradation model based on the maximum likelihood method, two dimensional Wiener degradation model based on the maximum likelihood method and the method we proposed where $\mu_1$ and $\sigma_1^2$ are parameters to support bearing temperature, $\mu_2$ and $\sigma_2^2$ are parameters to reducer rotor support bearing clearance and $\rho$ is the correlation coefficient between the two.

4.1.1 One dimensional Wiener degradation model based on MLE

The parameters of the support bearing temperature and the reducer rotor support bearing clearance are estimated by MLE, results are shown in Table 2

**Table 2.** Parameters estimator of one dimensional Wiener degradation model based on MLE.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>$\mu_1$</th>
<th>$\sigma_1^2$</th>
<th>$\mu_2$</th>
<th>$\sigma_2^2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Estimator</td>
<td>0.0070</td>
<td>0.0091</td>
<td>2.714×10^{-5}</td>
<td>9.928×10^{-8}</td>
</tr>
</tbody>
</table>

Bringing estimated results of parameter into one dimensional Wiener degradation model, the reliability of support bearing temperature is 0.8370 in 10000h, and the reliability of reducer rotor support bearing clearance is 0.8032 in 10000h. Because when one of the two parameters reaches its failure threshold, the steam turbine pump fails. So choose the result which reach its failure threshold first as reliability assessment result of steam turbine pump. In this example, the assessment of reducer rotor support bearing clearance is taken as result of steam turbine pump, namely, the reliability assessment of steam turbine pump is 0.8032 when the working time reach 10000h. The reliability curve is shown in Figure 1.
4.1.2 Two dimensional Wiener degradation model based on MLE

**Table 3.** Parameters estimator of two dimensional Wiener degradation model based on MLE.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>$\mu_1$</th>
<th>$\sigma_1^2$</th>
<th>$\mu_2$</th>
<th>$\sigma_2^2$</th>
<th>$\rho$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Estimator</td>
<td>0.0797</td>
<td>0.6043</td>
<td>1.500×10^{-4}</td>
<td>2.000×10^{-6}</td>
<td>0.7997</td>
</tr>
</tbody>
</table>

Figure 1. The reliability curve of steam turbine pump- One dimensional Wiener degradation model based on MLE.

Figure 2. The reliability curve of steam turbine pump- Two dimensional Wiener degradation model based on MLE.
Stable measurement is used to measure two parameters. Considering the correlation between these two parameters, the results of $\mu_1, \sigma_1^2, \mu_2, \sigma_2^2$ and $\rho$ are derived by bringing the data of two parameters into formula (10)-(12). Results are shown in Table 3.

Bringing the parameter estimator into formula (5), the reliability of steam turbine pump is obtained, it is 0.6376 at 10000h. The reliability curve is shown in Figure 2.

### 4.1.3 Two dimensional Wiener degradation model based on wear model

Bringing the data of two parameters into formula (12) (21), the results of $\mu_1, \sigma_1^2, \mu_2, \sigma_2^2$ and $\rho$ are obtained. Results are shown in Table 4.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>$\mu_1$</th>
<th>$\sigma_1^2$</th>
<th>$\mu_2$</th>
<th>$\sigma_2^2$</th>
<th>$\rho$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Estimator</td>
<td>0.0823</td>
<td>0.6043</td>
<td>1.610\times10^{-4}</td>
<td>2.000\times10^{-6}</td>
<td>0.8956</td>
</tr>
</tbody>
</table>

Bringing the parameter estimator into formula (22), the reliability of steam turbine pump at 10000h is obtained, which is 0.6920. The reliability curve is shown in Figure 3.

### 4.2 Comparison and analysis

Taking parameters estimator of three methods into their reliability functions respectively, the reliabilities at 10000h, are obtained, then calculate the relative error based on index. As shown in the Table 5, the reliability curves of the three methods are shown in the Figure 4.

<table>
<thead>
<tr>
<th>Method</th>
<th>R</th>
<th>Relative Error</th>
</tr>
</thead>
<tbody>
<tr>
<td>One dimensional Wiener degradation model based on MLE</td>
<td>0.8032</td>
<td>14.74%</td>
</tr>
<tr>
<td>Two dimensional Wiener degradation model based on MLE</td>
<td>0.6376</td>
<td>8.91%</td>
</tr>
<tr>
<td>Two dimensional Wiener degradation model based on wear model</td>
<td>0.6920</td>
<td>1.14%</td>
</tr>
</tbody>
</table>
Figure 4. The reliability curves of the three methods.

Comparing and analyzing the reliability calculation results and reliability curves of the three methods, it shows: the relative error of one dimensional Wiener degradation model based on MLE is the maximum which is 14.74%, followed by two dimensional Wiener degradation model based on MLE which is 8.91%. The minimum is the method proposed in this paper, which is 1.14%. It can be seen that the method proposed in this paper is the closest to the real index. From the Fig.4, the reliability falling speed becomes faster over time. As time goes by, support bearing temperature showed a fluctuating upward trend, which will increase the wear of metal components. Then reliability will decrease. Therefore, the method proposed in this paper is more in line with the actual situation.

5 Conclusion

(1) In practical engineering, more than one parameter affects the life of the product. When assess the reliability of the product, only considering one parameter to estimate the whole product is not comprehensive. The evaluation results of the multivariate degradation process are more in line with the actual situation than one dimensional degradation process.

(2) In this paper, from the point of view of two performance parameters, combined with the theory of random degradation, a model of two dimensional Wiener stochastic degradation model is proposed based on the wear model for the products which have a wear process and uncertain stochastic degradation processes. The two dimensional Wiener degradation model is optimized by the method proposed in this paper in a certain extent.

(3) From the result of steam turbine pump reliability assessment, compared to the results of one dimensional Wiener degradation model based on MLE and two dimensional Wiener degradation model based on MLE, the method proposed in this paper has the minimum relative error which is 1.14% on the reliability 0.7 at 1000h. Thus the method proposed in this paper is more in line with the actual situation and more reliable.
Figure 4. The reliability curves of the three methods.

Comparing and analyzing the reliability calculation results and reliability curves of the three methods, it shows: the relative error of one dimensional Wiener degradation model based on MLE is the maximum which is 14.74%, followed by two dimensional Wiener degradation model based on MLE which is 8.91%. The minimum is the method proposed in this paper, which is 1.14%. It can be seen that the method proposed in this paper is the closest to the real index. From the Fig.4, the reliability falling speed becomes faster over time. As time goes by, support bearing temperature showed a fluctuating upward trend, which will increase the wear of metal components. Then reliability will decrease. Therefore, the method proposed in this paper is more in line with the actual situation.

5 Conclusion

(1) In practical engineering, more than one parameter affects the life of the product. When assess the reliability of the product, only considering one parameter to estimate the whole product is not comprehensive. The evaluation results of the multivariate degradation process are more in line with the actual situation than one dimensional degradation process.
(2) In this paper, from the point of view of two performance parameters, combined with the theory of random degradation, a model of two dimensional Wiener stochastic degradation model is proposed based on the wear model for the products which have a wear process and uncertain stochastic degradation processes. The two dimensional Wiener degradation model is optimized by the method proposed in this paper in a certain extent.
(3) From the result of steam turbine pump reliability assessment, compared to the results of one dimensional Wiener degradation model based on MLE and two dimensional Wiener degradation model based on MLE, the method proposed in this paper has the minimum relative error which is 1.14% on the reliability 0.7 at 1000h. Thus the method proposed in this paper is more in line with the actual situation and more reliable.

References

18. G. Jin, Reliability Technology based on Degradation (Beijing, China, 2014)