

The relevance of non-stationarities and non-Gaussianities in vibration fatigue

Martin Česnik¹, Janko Slavič^{1,*}, Lorenzo Capponi², Massimiliano Palmieri², Filippo Cianetti², and Miha Boltežar¹

¹University of Ljubljana, Faculty of Mechanical Engineering, 1000 Ljubljana, Slovenia

²University of Perugia, Department of Engineering, 06125 Perugia, Italy

Abstract. In classical fatigue of materials, the frequency contents of dynamic loading are well below the natural frequencies of the observed structure or test specimen. However, when dealing with vibration fatigue the frequency contents of dynamic loading and structure's dynamic response overlap, resulting in amplified stress loads of the structure. For such cases, frequency counting methods are especially convenient. Gaussianity and stationarity assumptions are applied in frequency-domain methods for obtaining dynamic structure's response and frequency-domain methods for calculating damage accumulation rate. Since it is common in real environments for the structure to be excited with non-Gaussian and non-stationary loads, this study addresses the effects of such dynamic excitation to experimental time-to-failure of a structure.

Initially, the influence of non-Gaussian stationary excitation is experimentally studied via excitation signals with equal power density spectrum and different values of kurtosis. Since no relevant changes of structure's time-to-failure were observed, the study focused on non-stationary excitation signals that are also inherently non-Gaussian. The non-stationarity of excitation was achieved by amplitude modulation and significantly shorter times-to-failure were observed when compared to experiments with stationary non-Gaussian excitation.

Additionally, the structure's time-to-failure varied with the rate of the amplitude modulation. To oversee this phenomenon the presented study proposes a non-stationarity index which can be obtained from the excitation time history. The non-stationarity index was experimentally confirmed as a reliable estimator for severity of non-stationary excitation. The non-stationarity index is used to determine if the frequency-domain methods can safely be applied for time-to-failure calculation.

1 Introduction

Before its exploitation a product (structure) must undergo a number of tests to prove its durability when exposed to harsh environmental conditions (vibrations, temperature, humidity, etc.). When discussing product's resistance to vibrations an automotive, aerospace and other testing standards [1] specify vibration loads that should be applied to a product in a controlled laboratory conditions via electro-magnetic shaker. Potential failure of product during vibration testing mainly occurs due to wear or fatigue fracture. In such cases of fatigue failure, the damage accumulation is not directly correlated to vibration load, but is rather coupled in frequency domain with structure's dynamic properties [2].

Thus, when dealing with vibration fatigue of structure under random vibration loads the counting methods in frequency domain (Dirlik [3], Tovo-Benasciutti [4]) are significantly more applicable, computationally effective and faster [5] compared to counting methods in time domain (rainflow, range count), especially when long time-histories need to be evaluated. Fatigue life estimation with frequency counting method is based on power spectral density (PSD) function of structure's stress response and properties of multiaxial stress criterion [6, 7]. Inherently to this, a frequency counting methods assume signal's stationarity [8]. Furthermore, due to reasons of analytical deduction, an additional assumption of Gaussian nature

of stress signal should be sufficed. When both assumptions are respected, the frequency methods give reliable fatigue life estimation [9].

Considering standard vibration testing with random signal with given frequency profile both assumptions for frequency domain methods are satisfied. However, when dealing with real service loads or environment conditions, the non-Gaussian and non-stationary signals are commonly observed. To what extent does the invalidity of those assumptions result on fatigue estimation has been studied from different aspects in classical [10, 11] and vibration fatigue. In latter a non-Gaussian and non-stationary excitation signal is mechanically filtered by dynamic structure. An influence of non-Gaussian excitation to response signal and fatigue life was numerically investigated by Braccesi *et al.* [12], Rizzi *et al.* [13] and Kihm *et al.* [14], who used kurtosis and skewness as estimators of non-Gaussianity. Non-Gaussianity was also studied for vibration fatigue of composite structures [15] and MIMO test systems [16].

This manuscript presents an experimental and numerical analysis of non-Gaussianity and non-stationarity on vibration fatigue. Firstly, a dynamic structure of Y-shaped specimen [17] was experimentally excited with random stationary Gaussian signal to obtain fatigue parameters of used aluminium alloy. Secondly, a number of Y-specimens was excited with different sets of random signals, obtained by combining different kurtosis values and non-stationarities. As the non-

* Corresponding author: janko.slavic@fs.uni-lj.si

stationary non-Gaussian excitation was experimentally shown to be significantly more damaging compared to stationary non-Gaussian [18] the research later focused on experimental and numerical evaluation of non-stationarity rate of excitation signal. In this manuscript a run-test method [19] is proposed to obtain a non-stationarity index γ [20]. Its applicability will be tested on a large number of fatigue tests and the relation between the amplitude-modulated non-stationarity and time-to-failure will be researched.

2 Theoretical background

In this chapter a condensed review of fundamental theory will be presented that is later applied to actual experimental data. Firstly, methods for identifying non-Gaussianity and non-stationarity of the random signal will be shown. Secondly, general equations of motion for dynamic system are presented, which result in stress response PSD. Finally, a Tovo-Benasciutti frequency counting method is presented, which is used to obtain damage accumulation from stress response PSD.

2.1. Random signal properties

Given a discrete time-series of random process as $\mathbf{x} = [x_1, \dots, x_i, \dots, x_n]$, its j -th central moment M_j and mean value μ are given as:

$$M_j = \frac{1}{n} \sum_{i=1}^n (x_i - \mu)^j, \quad (1)$$

$$\mu = \frac{1}{n} \sum_{i=1}^n x_i \quad (2)$$

and are based on Probability Density Function $P(x)$ (PDF). The PDF of Gaussian process is defined by mean value and second central moment (variance) of the process. For PDF definition of non-Gaussian processes a higher number of parameters is needed, introducing

kurtosis k_u as a measure of non-Gaussianity and defined as:

$$k_u = M_3/M_2^{3/2}, \quad (3)$$

which characterizes the sharpness of the PDF peak and the width of the PDF tails. By definition, Gaussian process has kurtosis of 3. Non-Gaussian processes with high peak excursions have kurtosis higher than 3.

On the other hand, quantification of non-stationarity in signal is not that straightforward, due to nature of non-stationarity itself. However, certain methods exist that monitor the changes in signal's statistical properties, which are for stationary process constant. Run-test [8] is a non-parametric method that divides a signal in time windows and calculates a variation of a chosen statistical variable over the whole signal. For each time window a chosen variable is met with a criterion related to whole signal; in presented study a condition was defined as:

$$V(n) = \begin{cases} 1; & |R_W(n) - R_T| > \sigma_R \\ 0; & |R_W(n) - R_T| \leq \sigma_R \end{cases} \quad (4)$$

where $R_W(n)$ is a RMS value of a n -th window, R_T a RMS value of the whole signal and σ_R is a standard deviation of all window RMSs, as illustrated on signal time history on Fig. 1. A *run* is a sequence of identical observations V , followed and preceded by different observation. Too many or too little runs in a whole signal is a proof of signal's non-stationarity. If probability of observation 1 or 0 is equal for each window, N_i is a number of i observations and N is a total number of windows, then a mean value μ_r and variance σ_r^2 of runs is:

$$\mu_r = \frac{2 N_0 N_1}{N} + 1, \quad \sigma_r^2 = \frac{2 N_0 N_1 (2 N_0 N_1 - N)}{N^2 (N - 1)}. \quad (5)$$

Any difference of actual number of runs r from expected mean indicates a non-stationarity in signal. If a number of runs lays outside $\mu_r \pm \sigma_r$, a signal is considered non-stationary. Additionally, a non-stationarity index γ is defined as:

$$\gamma = r/\mu_r \quad [\%]. \quad (6)$$

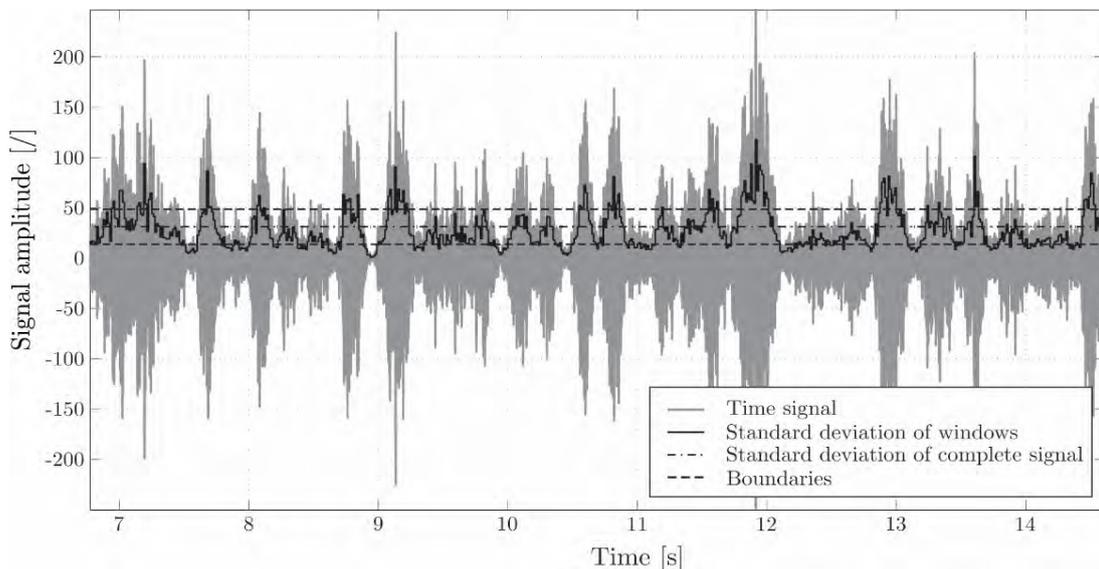


Fig. 1. Run-test evaluation of a non-stationary time signal.

2.2. Structural dynamics

Flexible multi-degree-of-freedom structures respond to force excitation by respecting the equation of motion [21]:

$$\mathbf{M} \ddot{\mathbf{x}}(t) + \mathbf{D} \dot{\mathbf{x}}(t) + \mathbf{K} \mathbf{x}(t) = \mathbf{F}(t). \quad (7)$$

In Eq. (7) \mathbf{M} , \mathbf{D} and \mathbf{K} present mass, damping and stiffness matrices, respectively; \mathbf{x} and \mathbf{F} are displacement and excitation force vectors. This coupled system of differential equations can be decoupled into

$$\mathbf{I} \ddot{\mathbf{q}}(t) + \mathbf{I} [2\xi\omega_0] \dot{\mathbf{q}}(t) + \mathbf{I} [\omega_0^2] \mathbf{q}(t) = \Phi^T \mathbf{F}(t), \quad (8)$$

by introducing modal coordinates $\mathbf{x} = \Phi \mathbf{q}$, where Φ is a modal matrix, consisting of mode shapes. ω_0 and ξ are natural frequency and damping ratio vectors, respectively. By solving eigenvalue problem to obtain r natural frequencies and modeshapes, uncoupled system of equations yields frequency response function on j^{th} position for excitation on k^{th} position:

$$H_{jk}(\omega) = \sum_{r=1}^n \frac{\phi_{jr} \phi_{kr}}{\omega_r^2 - \omega^2 + 2i\xi_r \omega_r \omega}. \quad (9)$$

Combining response functions into response function matrix and knowing stress states of mode shapes, one can obtain stress response power spectral density (PSD) for given excitation PSD $\mathbf{S}_{ff}(\omega)$ as:

$$\mathbf{S}_{\sigma\sigma}(\omega) = \mathbf{H}_{\sigma f}^*(\omega) \mathbf{S}_{ff}(\omega) \mathbf{H}_{\sigma f}^T(\omega). \quad (10)$$

2.3. Damage accumulation

Continuing from stress response PSD $\mathbf{S}_{\sigma\sigma}(\omega)$ an equivalent stress PSD $\mathbf{S}_{eq}(\omega)$ can be quickly obtained [22]. To employ frequency methods for fatigue calculation, m -th spectral moment should be defined [7]:

$$\lambda_m = \int_0^{\infty} \omega^m S_{eq}(\omega) d\omega. \quad (11)$$

Depending on the frequency method, a damage accumulation is a function of a list of spectral moments and material fatigue parameters C and b , as included in Basquin's equation $\sigma = C N^{-1/b}$ [23]. In this research, a Tovo-Benasciutti method [4] is proposed, that obtains damage accumulation D using following equation

$$D = (B_{TB} + (1 - B_{TB})\alpha_2^{B_{TB}-1})\alpha_2 D_{NB}, \quad (12)$$

where B_{TB} is a factor obtained from spectral moments $\lambda_0, \lambda_1, \lambda_2$ and λ_4 . D_{NB} is a damage for narrow band stress signal and depends on spectral moments ($\lambda_0, \lambda_1, \lambda_2, \lambda_4$) and material fatigue parameters (b, C) [3, 4].

3 Non-Gaussianity vs. non-stationarity

The first part of the study focuses on non-Gaussianity and non-stationarity of random excitation signal and its influence on actual vibration fatigue life. For this purpose, a Y-shaped specimen is used, Fig. 2. Its geometry consists of three beams that are arranged at 120° angles around the main axis and have a rectangular cross-section of 10×10 mm. The Y-shaped specimens

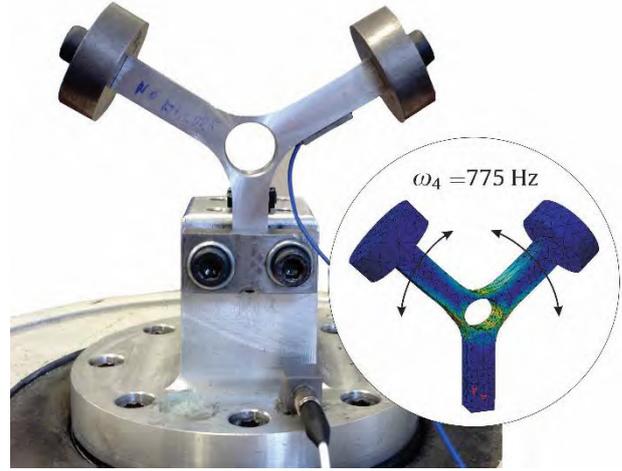


Fig. 2. Fixed Y-specimen with excited modeshape.

were made from the aluminium alloy A-S8U3; additional steel dead-weights with a mass of 52.5 g were added for natural-frequency tuning. The specimen was attached to electro-dynamic shaker and excited with flat-shaped force PSD profile (Fig. 3) with frequency range 600-850 Hz so that specimen's 4th natural frequency of 775 Hz lied within excited frequency band.

The procedure for evaluating non-Gaussianity and non-stationarity is following: first a set of specimens is excited with Gaussian stationary signals with flat PSD profiles at different amplitude levels (Fig. 3). By minimizing error between experimental and numerical fatigue lives material fatigue parameters C and b are obtained. Secondly, random signals with similar PSD profiles but different kurtosis and non-stationarities (Tab. 1) are generated and applied to the Y-specimens. Influence of non-Gaussianity and non-stationarity is then studied by comparing actual and predicted fatigue lives for given excitation signal type.

Tab. 1. Excitation signal types

Nr.	Signal type	k_u
1.	Gaussian stationary	2.96
2.	Non-Gaussian stationary	7.36
3.	Non-Gaussian stationary	5.43
4.	Non-Gaussian non-stationary	7.08

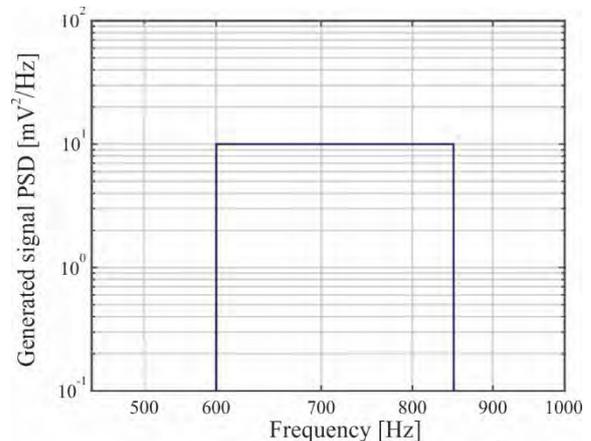


Fig. 3. Flat PSD profile with amplitude level 10 mV²/Hz.

Four Y-shaped specimens were excited with random stationary Gaussian signal until fatigue failure occurred. The obtained fatigue lives are presented in Fig. 4. In order to obtain fatigue material parameters a numeric model was built and validated (Fig. 5). A function for numerical minimization of numerical error was proposed as:

$$\Delta T(b, C) = \sum_i (\log_{10} T_{act,i} - \log_{10} T_{est,i}(b, C))^2, \quad (13)$$

where i denotes a single test specimen, T_{act} is the measured fatigue life and T_{est} is the estimated fatigue life of the specimen based on the numerical model. The minimization method showed strong convergence. Using the identified fatigue parameters, the Basquin's equation can be written as:

$$\sigma = 987.5 \cdot N^{-0.169}. \quad (14)$$

Once fatigue parameters were known, a number of samples were excited with signals, where non-Gaussianity and non-stationarity was combined according to Tab. 1. Time signals for signal types 3. and 4. with identical PSD profiles are presented in Figs. 6 and 7. The excitation force PSD level was precedently determined by measuring acceleration response of shaker's armature without Y-specimen [18]. Non-stationary signal was generated using amplitude modulation of stationary signal with beta-distribution signal [18, 20].

A total of nine Y-shaped specimens were tested under non-Gaussian excitation, three for each signal type 2-4. In order to evaluate the influence of the kurtosis on the fatigue life of tested specimens, the fatigue parameters

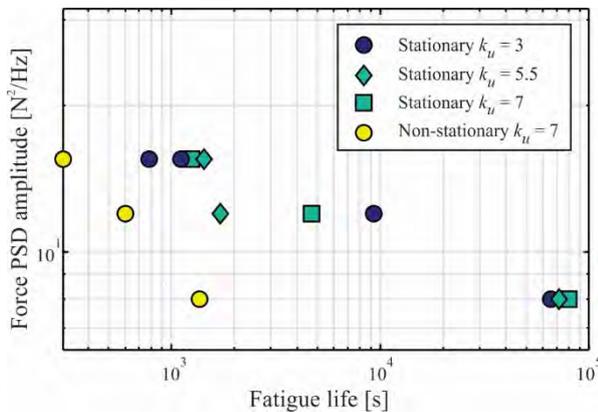


Fig. 4. Experimental fatigue lives.

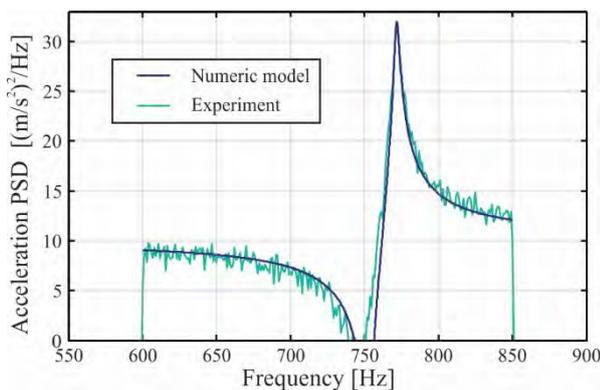


Fig. 5. Numerically and experimentally obtained response acceleration PSD.

obtained under the Gaussian condition are also used for a numerical estimation of the fatigue life for the case of non-Gaussian excitation. In order to investigate when it is justified to apply Gaussian-based counting methods to

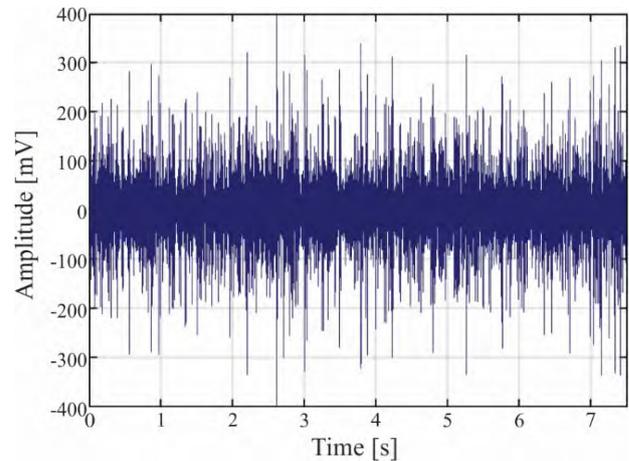


Fig. 6. Stationary non-Gaussian signal with $k_u = 7$.

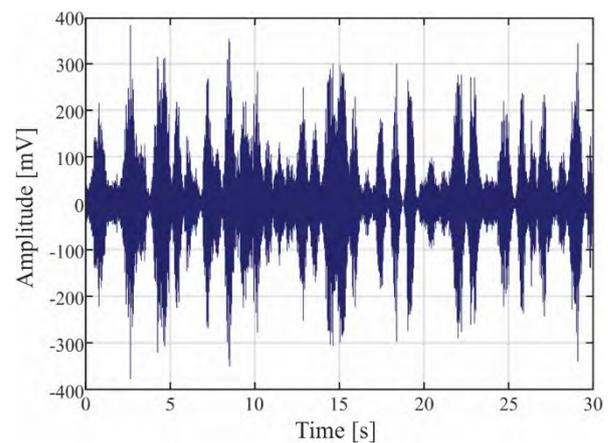


Fig. 7. Non-stationary non-Gaussian signal with $k_u = 7$.

non-stationary excitation, the Tovo-Benasciutti counting method was also used in the case of the non-Gaussian excitations.

A comparison between the experimental and calculated fatigue lives is shown in Fig. 8. From Fig. 8 it is noticeable that the stationary, non-Gaussian excitation differs only slightly if compared to the calculated fatigue life. In contrast to this case, for the case of non-stationary non-Gaussian excitation, the comparison shows how the difference between the calculated fatigue lives and the actual fatigue lives is significant. From this comparison one can conclude that for the case of stationary excitation the use of standard frequency-counting methods [9] available in the literature gives reliable results comparable to reality, while in the case of strongly non-stationary signals the use of the same counting methods supplies uncorrected results. Also, Fig. 4 shows the relation between the excitation force PSD amplitude and the experimental fatigue life; again, the non-stationary experiments clearly differentiate from the stationary experiments.

The latter difference between the calculated and measured fatigue lives arises due to the non-Gaussianity of the stress response. For this reason, a piezo-electric strain gauge was applied on the specimen's beam, as shown in Fig. 2, to monitor the stress response. For the case of stationary non-Gaussian loadings the kurtosis of the stress is always around the value 3, confirming that due to the stationarity of the excitation, the response of the structure is Gaussian. However, for the case of non-stationary non-Gaussian loadings the output kurtosis is significantly higher, although it is still lower than the kurtosis of the input signal. In any case, we can conclude that if the input signal is quasi-stationary, the output kurtosis always tends to the Gaussianity; however, if the input signal is non-stationary, the stress response remains strongly non-Gaussian and leads to shorter fatigue lives than expected.

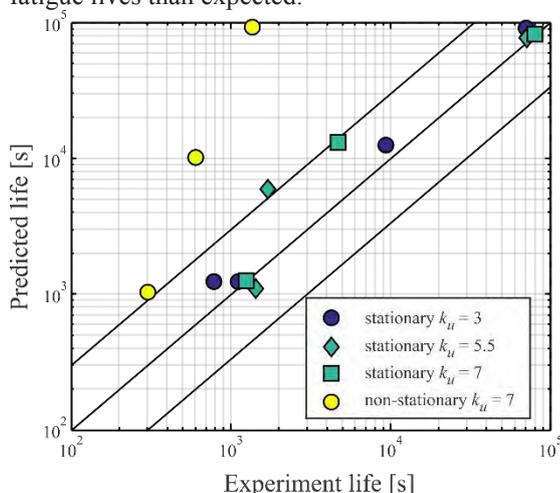


Fig. 8. Experimental and calculated fatigue lives.

4 Non-stationarity index

The following section focuses on quantification of non-stationarities in excitation signal and on identification of non-stationary signals that result in reduced vibration fatigue life.

4.1. Signal generation

In order to investigate this first a set of time signals with different non-stationarity rates was obtained. For the bulk of physical phenomena the non-stationarity is exhibited as the time variance of a signal's power; the fluctuations in signal's frequency content are less commonly observed.

Therefore, beta-distribution amplitude modulation of a stationary signal with flat-shaped PSD profile was initially performed with a carrier wave, as proposed in Sec. 3 (Fig. 7) and described in detail in [14] and [18].

In the next step the initial carrier wave with time duration of 30 minutes was then squeezed by a factor of 2 and again multiplied with flat-profiled stationary signal.

This signal was denoted as SQ-2, whereas the amplitude modulated signal with original (non-squeezed carrier wave) was denoted as SQ-1. In a similar manner, additional 5 nonstationary signals were generated for

different squeezing factors 4, 10, 50, 500 and 10000. After squeezing, each signal was repeated to reach the

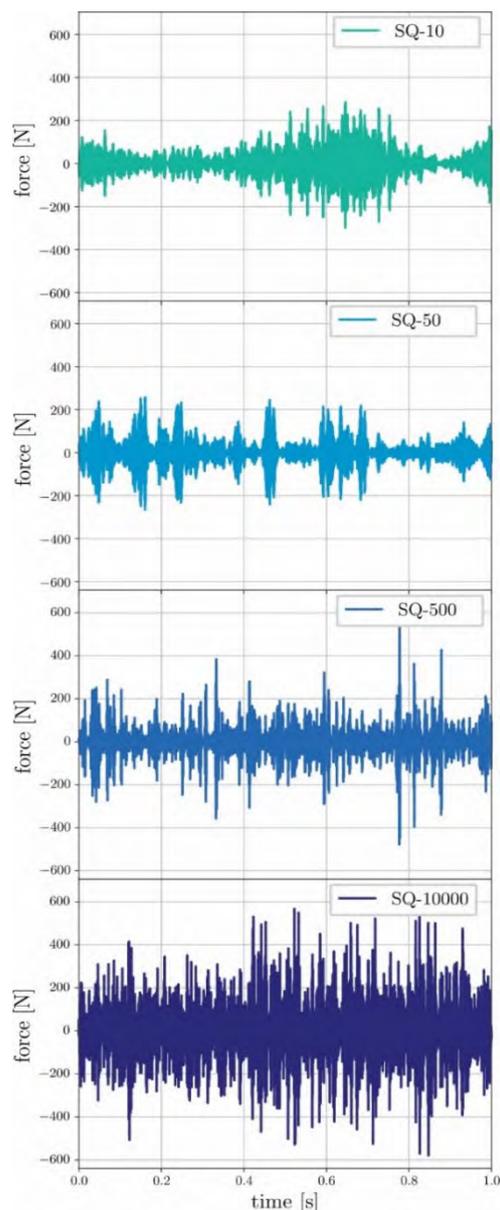


Fig. 9. Time history of measured excitation signals SQ-10, SQ-50, SQ-500 and SQ-10000 with PSD level of $13.5 \text{ N}^2/\text{Hz}$.

time length of 30 minutes. All time signals had the same PSD, the same time length, the same kurtosis, but different levels of non-stationarity. Squeezed signals SQ-10, SQ-50, SQ-500 and SQ-10000, that were measured on electro-dynamic shaker are presented in Fig. 9.

4.2. Signal evaluation with run-test method

Here, the signals later used for Y-specimen excitation and with PSD level of $13.5 \text{ N}^2/\text{Hz}$ are evaluated with two-sided run-test method, presented in Sec. 2.1 and Fig. 1. As known [3] run-test method is sensitive to the width of the windows, to which the signal is divided. Consequently, all 8 signals (7 non-stationary and 1 *de facto* stationary) were evaluated for different time lengths of dividing windows. In total seven time-window

widths were applied to the run-test, ranging from 0.005 to 1 s. In Tab. 2 the resulting non-stationarity indexes γ are given. Moreover, the influence of the window's

width is graphically presented in Fig. 10. According to Rizzi *et al.* [13] study the optimal window width is expected to be related to the period of

Tab. 2. Non-stationarity index γ for two-sided method: results in bold identify signal as stationary.

Signal type	Window width						
	0.005 s	0.01 s	0.0125 s	0.02 s	0.04 s	0.1 s	1 s
Stationary	96	99	100	101	102	99	72
SQ-10000	96	101	101	101	102	100	101
SQ-500	95	97	99	99	102	105	90
SQ-50	73	86	92	98	95	96	114
SQ-10	65	62	61	61	72	96	109
SQ-4	64	60	57	50	46	67	105
SQ-2	65	60	58	50	40	39	104
SQ-1	66	62	60	53	40	31	96

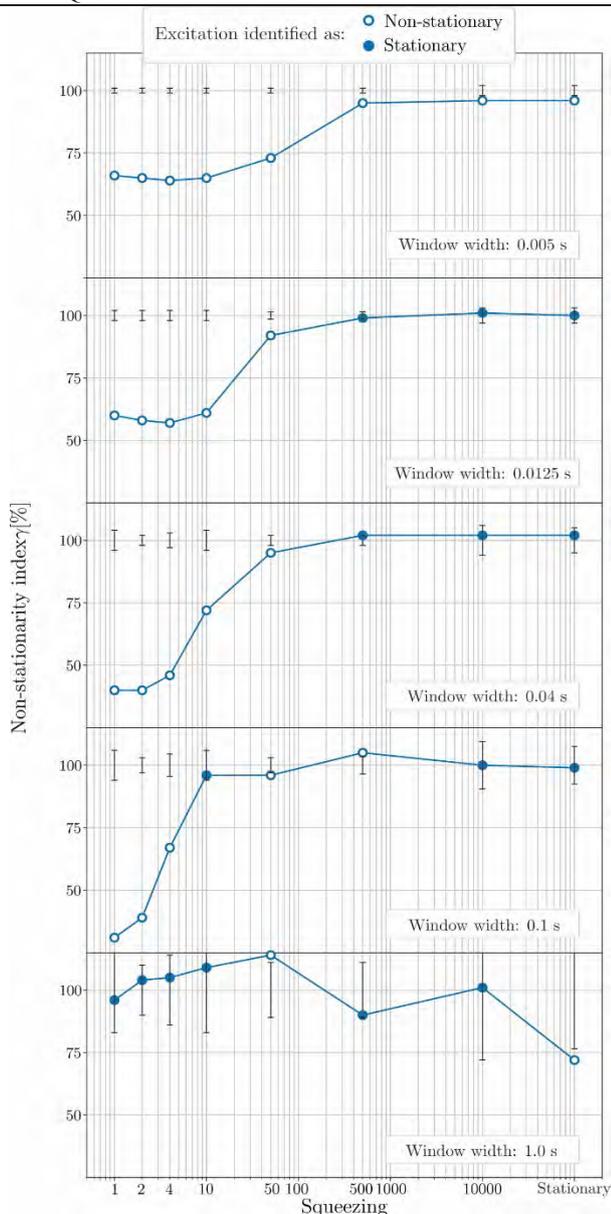


Fig. 10. Window width's influence on the non-stationarity index γ of measured excitation signal for two-sided run-test method with denoted confidence intervals.

the system's impulse response, *i.e.*, the time in which the response amplitude reduces to 10% of the initial value

[14]; in the case of the Y-specimen the period of the impulse response was experimentally determined to be in the range up to 0.2 s. By inspecting Fig. 10 a significant difference between low squeezing and high squeezing is observed; at a window width of 0.04 s the signals SQ-1 to SQ-4 were identified as non-stationary, while the SQ-500, SQ-10000 and also *de facto* stationary signal were identified as stationary. Similar results were found for other RMS values of the excitation signal.

4.2. Vibration fatigue testing

Here, the *de facto* stationary and squeezed signals SQ-1 - SQ-10000 were applied to the Y-specimen. According to a preliminary analysis of the excitation signals the non-stationarity index γ shows that the signals SQ-500, SQ-10000 can be considered as stationary and the signals SQ-1, SQ-2 and SQ-4 can be considered as non-stationary. This finding will now be tested against the actual vibration fatigue life.

For the sake of experimental comprehensiveness the time signals were applied to the Y-specimen at four different force PSD levels, as shown in Fig. 11. For each of the 19 combination pairs of excitation PSD level and signal type, two samples were teste. In total, 41 samples were broken. Certain load level and signal type combinations were left untested either due to instantaneous failure or due to the absence of failure after 2×10^7 load cycles.

The fatigue life for all tested specimens is given in Tab. 3. It is clear that squeezing the carrier wave and thus

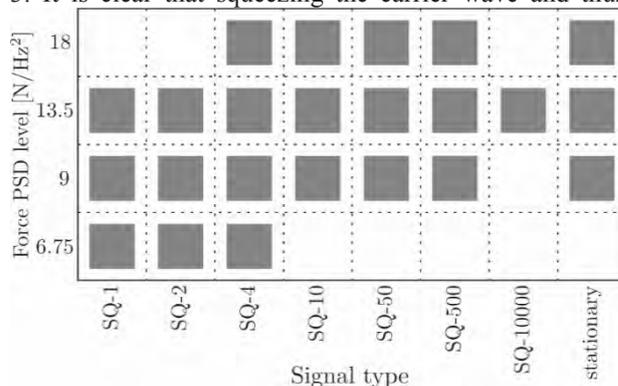


Fig. 11. Experimentally tested combinations of signal types and excitation levels.

changing the non-stationarity rate significantly changes the fatigue life, see Fig. 12. From Fig. 12 it is clear that **Tab. 3**. Experimental fatigue lives [s] of tested Y-specimens.

for the SQ-4 the fatigue life is significantly shorter than

Force PSD level [N ² /Hz]	Signal type							
	SQ-1	SQ-2	SQ-4	SQ-10	SQ-50	SQ-500	SQ-10000	Stationary
18	/	/	643	598	999	1624	/	3157
13.5	961	871	737	1175	1120	4069	6299	4428
9	857	907	899	1333	5234	6411	6309	4428
6.75	2364	2853	3279	3177	3722	>12600	/	>12600
	2994	2391	2899	3824	5894	/	/	/
	5112	2737	4429	/	/	/	/	/
	4865	4405	5435	/	/	/	/	/

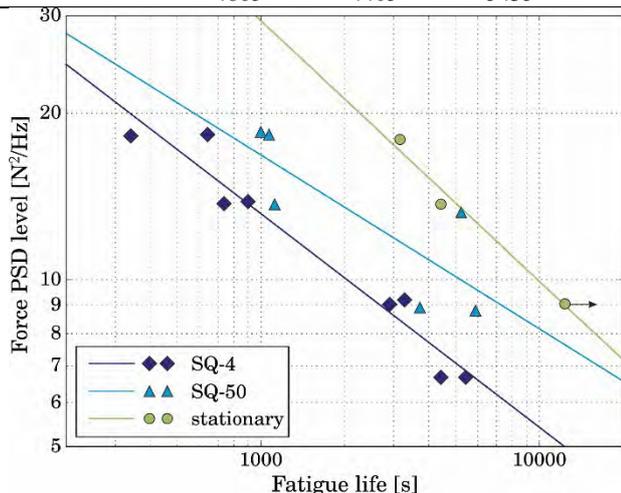


Fig. 12. Experimental fatigue life for the representative excitation signal types: SQ-4, SQ-50 and *de facto* stationary.

for the *de facto* stationary signal, while SQ-50 is in between.

Due to the considerable influence of the non-stationarity rate on the fatigue life only tests with an excitation force PSD level of 13.5 N²/Hz were possible on the complete set of generated non-stationary signals SQ-1 - SQ-10000 and on the *de facto* stationary signal, see Tab. 3. To better understand Fig. 12, a detailed analysis of the PSD level of 13.5 N²/Hz is shown in Fig. 13: one axis shows the fatigue life, the other axis shows the non-stationarity index. It was previously shown that the excitation signals from SQ-1 - SQ-4 can be considered as non-stationary, while signals SQ-500 and above can be considered as stationary. As all the time signals had the same PSD, the same time length, the same kurtosis, but different rates of non-stationarity one can conclude that of non-stationarity results in significant differences in fatigue life. The difference between non-stationary and stationary conditions is approximately 5-fold.

Fig. 14 shows the fatigue life normed to the fatigue life during stationary excitation. From the results of all 41 tested samples it is clear that the excitation identified as non-stationary resulted in a reduced fatigue life to approximately 20%. Signals that are not clearly stationary, nor are they non-stationary, have a fatigue life between the two groups. Based on presented results it is reasonable to conclude that non-stationarity index γ provides reliable results to distinguish between non-stationary excitation signals that do or do not reduce

vibration fatigue life when compared to stationary excitation.

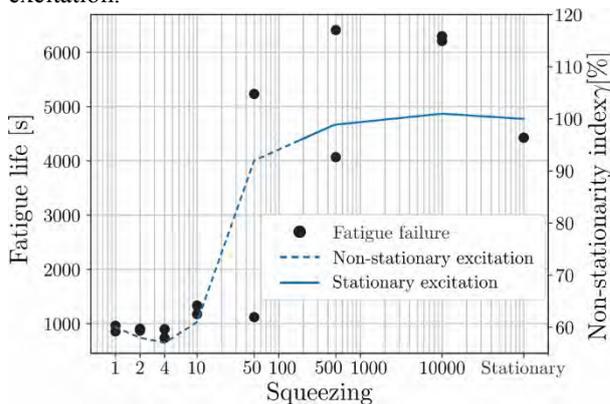


Fig. 13. Comparison of experimental fatigue lives for excitation PSD level of 13.5 N²/Hz and excitation signal's non-stationarity index γ for window width of 0.0125 seconds using two-sided run-test method.

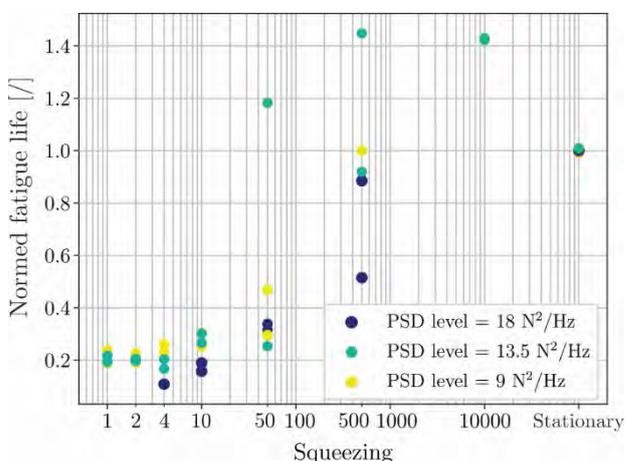


Fig. 14. Fatigue lives of Y-specimens, normed to fatigue life under *de facto* stationary excitation signal.

5 Conclusions

In the presented research the fatigue life of a simple Y-shaped specimen was investigated in order to determine how a change in the excitation kurtosis and stationarity affects the fatigue life of a real structure. Firstly, several experimental verifications of random excitation signals with the same PSDs, but with different kurtosis were performed. In the case of stationary random excitations, it was found that non-Gaussian signals with a stationary rate produced a Gaussian response, while in the case of

non-stationary random signals, the response of the structure is non-Gaussian. The obtained results show that the fatigue life due to amplitude-modulated non-stationary excitations is significantly shorter when compared to the fatigue lives obtained under the valid condition of stationarity. Moreover, it was found that if the non-Gaussian excitation is stationary, the calculated fatigue lives with classical frequency-counting methods are comparable to the fatigue lives under Gaussian excitation; therefore, justifying the use of frequency-counting methods, even if validated only in the case of Gaussian excitations. In contrast, for the case of burst, non-Gaussian excitation, the obtained fatigue life exhibits a significantly higher damage accumulation compared to the fatigue lives attained under Gaussian signals. For this reason, considering a non-stationary non-Gaussian excitation as Gaussian and, consequently adopting the classic frequency-counting methods may result in a wrong fatigue-life estimation.

To this end, a study later focused on identifying critical non-stationary amplitude-modulated in terms of actual fatigue life. Excitation is frequently non-stationary in terms of time-varying power and the question is what rate of non-stationarity can still be considered as stationary and how does the rate of non-stationarity effect the fatigue life? To answer this, additional experimental tests of Y-specimens were performed using squeezed signals with the same PSD and kurtosis, but different rates of non-stationarity. An enhanced method to identify the non-stationarity was proposed and resulted in a clear differentiation of the non-stationarity in the signal.

The signals that were identified as non-stationary resulted in a significantly shorter fatigue life of the sample than the ones that were identified as (or were de facto) stationary. Finally, the non-stationarity identification relates on the natural frequencies of the researched structure. However, if the non-stationarity is identified during the excitation, the resulting fatigue life was shown to significantly decrease (in this research to 1/5th).

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