

Prediction of leakage in the fixed mechanical seal

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Abstract. The questions of influence of the shape of contact surfaces on leakages through rubber seals in fixed connection of subassemblies are considered in the article. It is known from practice of operation of seals of various designs that the shape of contact surfaces and consequently also the shape of diagram of stresses in a contact zone considerably influences on value of leaks Linking leakage magnitude and distribution of contact stresses enables, firstly, more precisely calculate the amount of leakage for existing seals, and, secondly, to optimize the shape of the seals in their design in each case. As the result of experimental studies on the introduction of the rubber gasket ring fixed indenters different profiles found that by optimizing the shape of the indenter magnitude of leakage can be reduced by 10 times.

1 Introduction

Leakage through a circular fixed mechanical seal can be defined by the formula [1]

$$Q = \frac{\pi}{6 \ln R_1/R_2} \frac{\Delta p}{\eta} \psi_0 R_z^3 \exp\left(-\frac{3\sigma_n}{kE}\right) \quad (1)$$

where Q is leakage through the seal R_1 and R_2 - the outer and inner radii of gaskets; Δp is pressure drop; η is the viscosity of the sealing medium ψ_0 is the coefficient of micro-roughnesses form; R_z is the sealing surface roughness parameter; σ_n is the normal stress on the contact point; E is the seal modulus; k is the coefficient taking into account the specific features of the physical model 0.05 to 0.3.

Formula (1) derived from the Navier-Stokes equations for laminar flow of gas without considering the centrifugal forces. From the analysis of the above expression for leak detection, follows that they are largely dependent on the magnitude of the stresses in the zone of contact of the seal with the sealing surface. The magnitude of this stress is known [1- 4], which depends on the preload pressure p_{ko} and in some designs of seals depends on the drop pressure of sealed medium Δp . Usually in the formula (1) the average value of the normal stress is using [5-7].

From experimental practices of various designs of seals [8-10] is known that the shape of the contact surfaces and, consequently, the shape and stress distribution in the contact area significantly affects the amount of leakage. In literature, however, practically there is no information about the effect of contact stress distribution along the width of the contact area on leakage. Thus establishing a relation between leak size and distribution of contact stresses will allow firstly to better calculate the amount of leakage for existing seals

and secondly to optimize the shape of the seals in their design in each case.

2 Apparatus for investigations and test method

Scheme of apparatus for studying leakage through mechanical seal is shown in Fig. 1. The appearance of the elements of the structure with photographs of the ring indenter and their schemes are shown in Fig. 2.

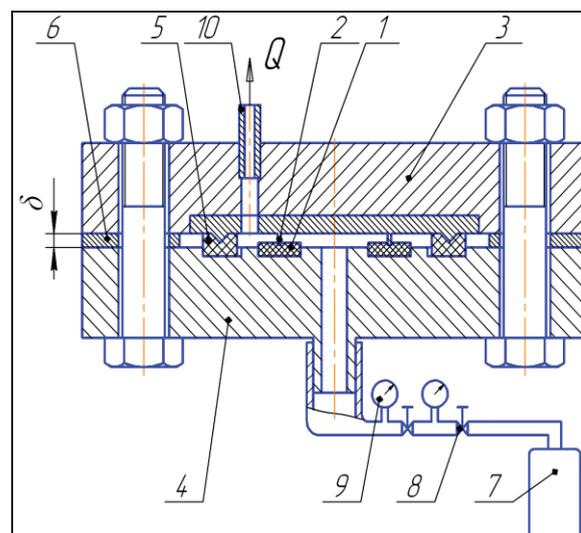


Fig. 1. The apparatus for leakage studying through mechanical seal.

The object of the study is a fixed mechanical ring seal 1. In tests, the rubber O-ring clamped between two steel flanges 3 and 4. In the inner cavity seal supplied pressurized air, 0 – 1.5 MPa. Air was supplied from a gas cylinder 7, where its pressure was 15 MPa through the gas reducer 8. Accuracy of adjustment and

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measurement of overpressure was 0.01 MPa. leakage measured from the outside of the gasket (10 fitting).

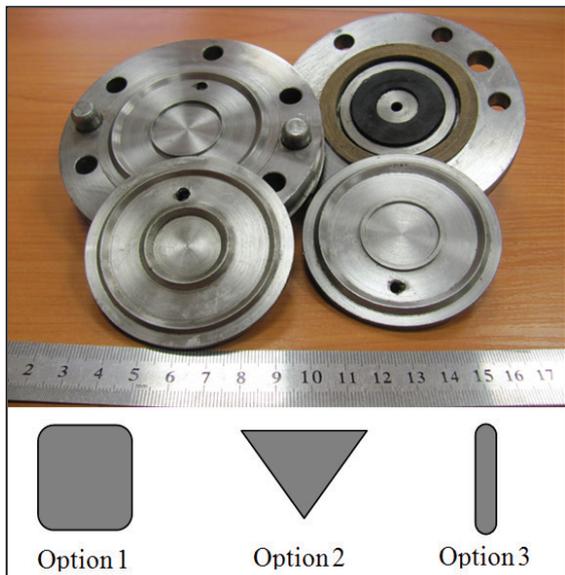


Fig. 2. Appearance of the elements of the structure and the scheme of indenters variants.

The dimension of the rubber O-ring with the rectangular section 1 is as follows: outer diameter of 36 mm, inner diameter of 16 mm and height of 4 mm. It was placed in an annular groove on the steel flange 3 with the depth of 2.6 mm and the diameter is equal to the diameter of the gasket and glued. In the opposite flange laid removable ring indenters 2 of different shapes (3 options, see Fig. 2).

In the first embodiment, it was a rectangular protrusion 1.8 mm wide with radii of 0.3 mm at the edges (width of the flat portion 1.2 mm). In the second embodiment, the protrusion section is an equilateral triangle with angles at the apex of 90 ° and the radius at the tip of 0.5 mm. In the third embodiment, it was rectangular protrusion 0.4 mm wide with the radius of 0.2 mm at the top. The roughness surface of protrusion corresponded to $R_a = 1.25 \mu\text{m}$. Static modulus of rubber was $E = 3.2 \text{ MPa}$. Average diameter of the protrusions in all cases was 25.8 mm, and the height was 1.8 mm. The preload pressure p_{ko} was created by six bolting joints which are spaced evenly over flanges. Movement was regulated and measured by instrumental measurement tiles 6 (see Fig. 1) with the accuracy of 0.01 mm.

During the test, the rubber O-ring was placed in the groove on the steel flange. By means of bolting and measuring plates 6 was set in the rubber specified minimum implementation δ of the annular protrusion – indenter, made from the first embodiment. Then, through the gas reducer in the internal cavity of the seal was applied the specified minimum air pressure and the leakage was measured. After this, the air pressure was increased and leakage measurement was repeated. After measuring the leakage over the entire range of pressures, the implementation value δ has been increased to the following amount, and all measurements were repeated.

3 Results of experimental studies

As the result of the experimental studies were obtained the dependence of leakage from excessive pressure at different values of the implementation of the protrusion in the rubber. These dependencies for the first variant form of the indenter are presented in Figures 3-5.

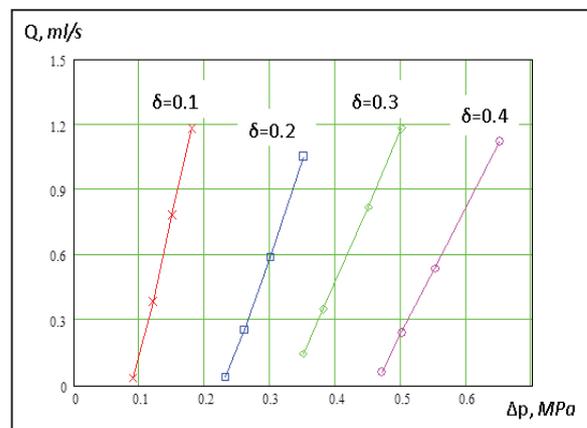


Fig. 3. Dependence of leaks from the pressure drop at different implementations δ in the rubber indenter made of embodiment 1.

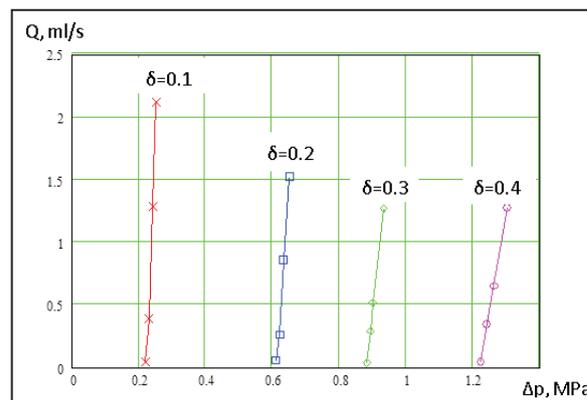


Fig. 4. Dependence of leaks on the pressure drop for various insertions of δ into the rubber.

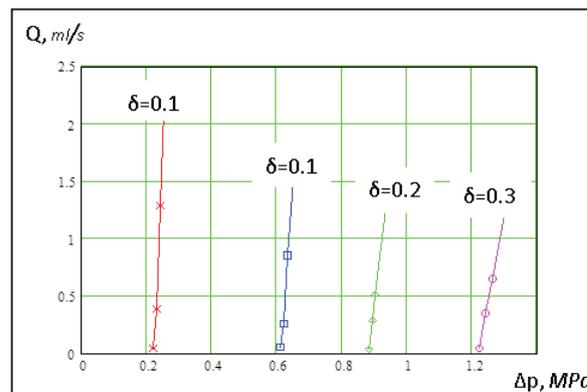


Fig. 5. Dependence of leakages on the pressure drop for various insertions of δ into the indenter rubber manufactured according to the variant 3.

Table 1. Results of geometric similarity coefficient calculation.

δ, mm	R_1, mm	R_2, mm	R_1/R_2	$\ln R_1/R_2$	$\left(\ln \frac{R_1}{R_2}\right)_1 / \left(\ln \frac{R_1}{R_2}\right)_j$
1st embodiment					
0.1	13.72	12.08	1.1358	0.12646	1
0.2	13.77	12.03	1.1446	0.13506	1
0.3	13.80	12.00	1.1500	0.13977	1
0.4	13.80	12.00	1.1500	0.13977	1
2nd embodiment					
0.1	13.20	12.60	1.0476	0.04650	2.72
0.2	13.30	12.50	1.0640	0.06204	2.17
0.3	13.50	12.30	1.0976	0.09313	1.50
0.4	13.60	12.20	1.1148	0.10868	1.29
3rd embodiment					
0.1	13.06	12.74	1.0251	0.02479	5.10
0.2	13.10	12.70	1.0315	0.03101	4.37
0.3	13.10	12.70	1.0315	0.03101	4.50
0.4	13.10	12.70	1.0315	0.03101	4.50

Analysis of the results showed that for all variants forms of indenters and for all values of the implementations of the indenter in the rubber observed linear dependence of the leakage of the sealed medium pressure drop that corresponds to the formula (1).

However, the obtained dependencies does not allow to compare the results of experiments with various embodiments indenters since radiuses R_1 and R_2 (macrogeometry), used in formula (1), in these three structures differ sharply. Values of these radii and the ratio $(\ln R_1/R_2)_1 / (\ln R_1/R_2)_j$ which may be called the geometric similarity ratio, in comparable embodiments with different implementations of the indenter in the rubber δ are given in table 1. The index j , here corresponds to the embodiment which is compared with the first embodiment, that is selected as the basic embodiment.

The use of geometric similarity coefficient allows lead dependencies obtained experimentally for different indenters to the basic embodiment (embodiment 1). This alignment makes it possible to eliminate the influence of all factors on the leakage except concentration of the stress created by the indenter in embodiments 2 and 3. From the leakage calculations regarding the similarity factor we can say leak in the second embodiment is approximately 2 times less than in the first (basic) embodiment and in the third embodiment, the difference reaches 10-times.

Analysis of the expression (1) allows determining the excess of the maximum stress σ_{max} over medium stresses σ_m . This can be accomplished by the use of the results of

the two series of experiments. In the first series for the base embodiment (first), $\sigma_{max} = \sigma_m$. In the second series, σ_{max} should significantly exceed the average stress, achieved for the second and third embodiments form indenters. Transforming the formula (1), we obtain

$$\sigma_{max} - \sigma_m = \frac{1}{3} \cdot k E \cdot \ln \left\{ \frac{Q_1}{Q_j} \cdot \frac{\Delta p_j}{\Delta p_1} \cdot \frac{\left(\ln \frac{R_1}{R_2}\right)_1}{\left(\ln \frac{R_1}{R_2}\right)_j} \right\}, \quad (2)$$

where the value

$$B = \frac{Q_1}{Q_j} \cdot \frac{\Delta p_j}{\Delta p_1} \cdot \frac{\left(\ln \frac{R_1}{R_2}\right)_1}{\left(\ln \frac{R_1}{R_2}\right)_j},$$

can be called the general similarity coefficient.

Value σ_m can be defined as

$$\sigma_m = E/\varepsilon, \quad (3)$$

where ε is the relative deformation which in this experiment can be defined as

$$\varepsilon = \delta/h, \quad (4)$$

where h is the thickness of the rubber gasket $h = 4 mm$.

Then, using the experimental values of the pressure drops and the related leak from Fig. 2 and of similar

Table 2. The calculation results of the experimental ratio σ_{max}/σ_m .

δ mm	Q_i ml/s	Q_j ml/s	Δp_i MPa	Δp_j MPa	B	ϵ	σ_m MPa	σ_{max} MPa	σ_{max}/σ_m
comparing the second embodiment with the base (first)									
0.1	1.280	0.640	0.24	0.18	4.08	0.025	0.08	0.155	1.93
0.2	1.260	0.540	0.93	0.44	2.40	0.050	0.16	0.207	1.29
0.3	1.270	0.724	1.30	0.88	1.78	0.075	0.24	0.271	1.13
comparing the third embodiment with the base (first)									
0.1	1.280	0.780	0.24	0.15	5.10	0.025	0.08	0.168	2.10
0.2	1.260	0.588	0.93	0.30	4.37	0.050	0.16	0.218	1.36
0.3	1.270	0.820	1.30	0.45	4.50	0.075	0.24	0.287	1.20

dependencies for indenters for embodiments 2 and 3, and taking $k = 0.05$, we obtain experimental ratio σ_{max}/σ_m . All results of these calculations are summarized in Table 2.

4 Conclusions

As the result of experimental studies on the implementation of circular indenters of various profiles in the rubber gasket fixed found that by optimizing the shape of the indenter, magnitude of leakage can be reduced by 10 times. Establishing relation between the leak and the size of the contact stress distribution allows more precisely calculate the amount of leakage for existing seals, as well as to optimize the shape of the seals in their design.

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