Multi-Path Signal Synchronization Model with Phase Ratio and Dispersion Constraints

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Abstract. Proper designs of offsets for signalized intersections in an urban arterial system can help improve the level of service (LoS) significantly. The MAXBAND model has been the most widely used approach for this purpose. In this paper, a MAXBAND model in which the lengths of phases in a cycle are variable is proposed. In other words, the lengths of phases in a cycle, as well as the cycle itself, are no longer fixed. Besides, the incorporation of traffic dispersion module in the proposed model allows that the travel times from upstream intersection to the downstream one are taken into account. Real-world application on an arterial system in Taiwan for evaluating the performance of the proposed model is conducted to validate the methodology. Actual traffic flow data are collected through on-site experiments. Results suggest that the improvements are around 44%, on average, in terms of total delay of the entire network.

1 Introduction
An effective signal control strategy is crucial in improving the LoS for coordinated signalized intersections. By adjusting the offsets of the coordinated intersections in an arterial system, the control delays and the stopping times of vehicles can be well controlled, thereby providing better LoS. The MAXBAND model, proposed by Morgan and Little1, is one effective approach for this purpose. The concept of the MAXBAND model is to maximize the total progression bandwidth of a two-way coordinated signalized system by adjusting the offsets at each intersection over a time interval.

The very first MAXBAND model was proposed by Little et al.2 in 1966. The model encompasses time constraints describing the relationship between the upstream and downstream intersections. Chang et al.3 proposed the MAXBAND-86 that extends Little’s model to solve multi-arterial closed network problems. Yet, neither model has considered the lead-lag left-turning phases and the queuing clearance times. Gartner et al.4 solved the problem by developing a multiband model that incorporates the left-turn phase sequence optimization and initial queue clearance times. The major contribution of multiband model resides in the consideration of the flow volume in the model.

Based on the multiband model, several extensions have been proposed thereafter. Stamatidis et al.5,6 proposed the Multiband-96 model, extending the multiband model to arterial networks. Lu et al.7 extended the multiband model by incorporating the travel time constraints with traffic dispersion module9. Zhang et al.10 improved Gartner’s model by relaxing the limitation of symmetrical progression. However, all these models above do not consider the turning flow from the minor legs crossing the arterial. In this case, the efficiency of the arterial system may increase, whereas that of the entire network may not necessarily. Most recently, Yang et al.11 proposed a multi-path progression model featuring the optimization of the phase sequences and the determination of critical paths in the associated network. This model can handle the intersections with high turning volumes on the minor legs by adding a new path through the arterial.

A major restriction in Yang’s model resides in that the length of the common cycle, as well as that of the phases, for the coordinated intersections are fixed. Such a restriction may possibly lead to unsatisfactory local solutions. Therefore, based upon this observation, an extension of their model by relaxing such restrictions is proposed so that the lengths of phases in a cycle, as well as the cycle itself, become variable. Such flexibilities can certainly lead to better solutions, compared to the fixed case. Besides, the incorporation of Robertson’s traffic dispersion module9 allows one to take into account the travel times from the upstream intersection to the downstream one, thereby providing more realistic results. Consequently, the resultant model becomes a mixed-integer quadratically constrained programming (MIQCP) problem which is NP-hard in essence. We then exploit Gurobi solver14 to search for an approximate feasible solution. Plus, empirical experiments are conducted for evaluating our methodology, and the results suggest that the performance of our model comes with an improvement being around 44% on average, in terms of total control delay per minute.
This is how the rest of the paper is organized. In Section 2, we first review the base model proposed by Yang et al.11, and then introduce the revised model thereafter. In Section 3, we elaborate on how the experiments as well as the numerical simulations are performed. Conclusions will be given in Section 4.

2 Model Specifications

In this section, the review of the multi-path progression model proposed by Yang et al.11, and then introduce the revised model. Thereafter, in Section 3, we elaborate on how the experiments as well as the numerical simulations are performed. Conclusions will be given in Section 4.

2.1. Multi-path progression model - A review

Variables to be used in the multi-path progression model are given in Table 1.

<table>
<thead>
<tr>
<th>Table 1. Notations</th>
</tr>
</thead>
<tbody>
<tr>
<td>$P(\bar{p})$</td>
</tr>
<tr>
<td>$b_p(b_p)$</td>
</tr>
<tr>
<td>$\varphi_p(\varphi_p)$</td>
</tr>
<tr>
<td>$\beta_{p,i,l}(\beta_{p,\bar{l},l})$</td>
</tr>
<tr>
<td>$w_{p,i}(w_{\bar{p},i})$</td>
</tr>
<tr>
<td>$\tau_i(\bar{\tau}_i)$</td>
</tr>
<tr>
<td>$t_i(t_{\bar{l}})$</td>
</tr>
<tr>
<td>$m_{p,i}$</td>
</tr>
<tr>
<td>$x_{l,m,i}$</td>
</tr>
<tr>
<td>$\phi_{l,i}$</td>
</tr>
</tbody>
</table>

The multi-path progression model proposed by Yang et al.11 is given below:

\[
\text{Max} \sum_p (\varphi_p b_p) + \sum_p (\varphi_p b_{\bar{p}}) \tag{1}
\]

s.t.

\[w_{p,i} + b_p \leq \sum_l \beta_{p,i,l} \phi_{l,i} \tag{2}\]

\[w_{\bar{p},i} + b_{\bar{p}} \leq \sum_l \beta_{\bar{p},\bar{l},l} \phi_{l,i} \tag{3}\]

\[\theta_i + r_{p,i} + w_{p,i} + t_i + m_{p,i} = \theta_{i+1} + r_{p,i+1} + w_{p,i+1} + \tau_{p,i+1} + m_{p,i+1} \tag{4}\]

\[-\theta_i + \bar{r}_{p,i} + w_{\bar{p},i} - \tau_{p,i} + \bar{t}_i + m_{\bar{p},i} = -\theta_{i+1} + \bar{r}_{p,i+1} + w_{\bar{p},i+1} + m_{\bar{p},i+1} \tag{5}\]

\[r_{p,i} \leq \sum_l \beta_{p,m,i} x_{l,m,i} \phi_{l,i} + M(1 - \beta_{p,m,i}) \quad \forall m \tag{6}\]

\[r_{p,i} + \bar{r}_{p,i} + \sum_l \beta_{p,l,i} \phi_{l,i} = 1 \tag{7}\]

\[r_{p,i} \leq \sum_l \beta_{p,m,i} x_{l,m,i} \phi_{l,i} + M(1 - \beta_{p,m,i}) \quad \forall m \tag{9}\]

\[r_{p,i} \leq \sum_l \beta_{p,m,i} x_{l,m,i} \phi_{l,i} + M(1 - \beta_{p,m,i}) \quad \forall m \tag{10}\]

\[r_{p,i} + \bar{r}_{p,i} + \sum_l \beta_{p,l,i} \phi_{l,i} = 1 \tag{11}\]

\[x_{l,m,i} = 0, \forall l \tag{12}\]

\[x_{l,m,i} + x_{m,i} = 1, \forall l \neq m; \forall i \tag{13}\]

\[x_{l,m,i} + x_{n,m,i} - 1, \forall l \neq m; \forall i \tag{14}\]

\[x_{l,m,i} + x_{n,m,i} = 1, \forall l \neq m; \forall i \tag{15}\]

\[x_{l,m,i} = 1, \forall l \neq m; \forall i \tag{16}\]

\[x_{l,m,i} - x_{i,m,i} = 0, \forall i \tag{17}\]

The decision variables include bandwidth $b_p(b_{\bar{p}})$, the interference variable $w_{p,i}(w_{\bar{p},i})$, the phase ratio $\phi_{l,i}$, the left(right) side red time $r_{p,i}(\bar{r}_{p,i})$, the offset $\theta_i$, the loop variable $m_{p,i}$, and the phase relative position variable $x_{l,m,i}$.

The parameters include the weight of bandwidth $\varphi_p(\varphi_{\bar{p}})$, the available phase parameter $\beta_{p,i,l}(\beta_{\bar{p},\bar{l},l})$, the travel time $t_i(\bar{t}_i)$, and the queue clearance time $\tau_{p,i}(\tau_{p,\bar{l}})$. $M$ is a penalty parameter.

The objective function (1) is to maximize the sum of bandwidths of outbound (\bar{p}) and inbound paths (\bar{P}). The weights $\varphi_p(\varphi_{\bar{p}})$ can be adjusted in accordance with the volumes of the associated paths. Here we have $\varphi_{\bar{p}} = \varphi_p = 1$.

Constraints (2) and (3) are interference constraints. They guarantee that the progression band of path $p(\bar{p})$ will only use the available green time at intersection $i$. Constraints (4) and (5) are loop constraints, representing the relationship of the intersection $i$ and $i+1$ while they are synchronized.

Constraints (6)-(17) are phase sequence constraints at each intersection so that the green band competition among different paths are controlled. Specifically, Constraints (6)-(11) are the boundary conditions for the left/right side red times of progression band. Constraints (12)-(17) ensure that the resulting phase sequence is feasible.

2.2. Revised model 1: Making $\phi_{l,i}$ a variable

In the progression model introduced in Section 2, the phase ratio $\phi_{l,i}$ is a constant. Here this restriction is relaxed and $\phi_{l,i}$ is made a variable. By doing so, constraints associated with $\phi_{l,i}$ become nonlinear in essence. The problem then becomes a nonlinear constrained mixed integer optimization problem, or more specifically, a mixed integer quadratically constrained programming (MIQCP) problem. Besides, constraints...
(15)-(17) will not be used, similar to the manipulation in Yang et al.\textsuperscript{11}

Along with the relaxation on the phase ratio, the restriction that the cycle length is also fixed is also relaxed. To do this, we add constraint (18) to ensure that the cycle length is now varying but bounded.

\[ \frac{1}{e} \leq Z \leq \frac{1}{f} \]

where \( Z \) is the reciprocal of the cycle length, and \( e (f) \) is the upper (lower) bound of cycle length. Based on (18), the travel time from intersection \( i \) to intersection \( i+1 \) can then be formulated as

\[ t_i = \frac{d_i}{v_i} Z \]

(19)

where \( d_i \) is the distance from outbound (inbound) intersection \( i \) to \( i+1 \); and \( v_i \) is the free flow speed of the link.

The sum of the phase lengths at any intersection must equal the cycle length; in other words, the total ratio of phases at an intersection must equal 1. Thus,

\[ \sum_i \phi_{ij} = 1, \forall i \]

(21)

To ensure that the resulting MIQCP is solvable, according to the model must come with lower bounds on the phase ratio variable \( \phi_{ij} \), to be given in (22). To correctly set the bounds for the ratio variable, we resort to the capacity equation discussed in Roess et al.\textsuperscript{15}, given by

\[ c_q = s_q \cdot \frac{\theta q}{C} \]

where \( c_q \) is the saturation flow rate for lane or lane group \( q \), \( \theta q \) is the effective green time for lane or lane group \( q \), and \( C \) is signal cycle length. This equation can be rewritten as \( \frac{c_q}{s_q} = \frac{\theta q}{C} \). Since the critical volume of lane \( V^c_q \) will never be bigger than the capacity \( c_q \), we then have \( \frac{\theta q}{C} = \frac{c_q}{s_q} \geq \frac{V^c_q}{s_q} \). Here, the ratio \( \frac{\theta q}{C} \) can be considered as the ratio of the phase length to the cycle length, which is also the ratio of phase(\( \phi_q \)). Consequently, we have

\[ \frac{\theta q}{C} = \phi_q = \frac{c_q}{s_q} \geq \frac{V^c_q}{s_q} \]

Therefore, the lower bounds for the phase ratio variable \( \phi_{ij} \) are given below:

\[ \phi_{ij} \geq \frac{V^c_i}{s_i} \cdot \frac{s_i}{s_j} \cdot \frac{1}{\Sigma_j j+1 \cdot 0.1}, \text{otherwise.} \]

(22)

Alternatively, the threshold 0.9 is set to evade over-saturation, so that the remaining one-tenth of the entire cycle can be used as further adjustments, if needed.

Therefore, the revised model, termed as RMPPM1, is given as follows:

\[ \text{RMPPM1} \quad \text{Max} \quad \sum_p (\phi_p b_p) + \sum_p (\phi_p b_p) \]

s.t. Eqs. (2) – (14), (18) – (22)

2.3. Revised model 2: adding traffic dispersion

In RMPPM1, the parameter \( t_i \) is mainly defined by the ratio of distance between the intersection to the downstream of the free flow speed of the link. In the development of MAXBAND model, there are two methods to process \( t_i \). One is to make it a constant, and the other is to set a boundary for it, see LP2 in Little et al.\textsuperscript{2}. Both methods have their disadvantages. For the first method, the real free flow speed might never be reached even when traffic is moderate to dense; and the second method requires new variables, thereby introducing more complexities to the problem. Based upon this, Lu et al.\textsuperscript{8} proposed a model that combined the multiband model proposed by Gartner et al.\textsuperscript{4} and the traffic flow dispersion model proposed by Robertson\textsuperscript{9}, so that the calculation of the link travel time can be more realistic.

In this study, we encompass the suggestion by considering the traffic dispersion module in the proposed RMPPM1, named RMPPM2. The travel time constraints (19)-(20) are then replaced by (23)-(24)

\[ t_i = \sum_{\tau = \text{Timefast}}^{\text{Timel slow}} T_i (1 - F) T_i - \text{Timefast} \cdot Z \]

(23)

where \( F = \frac{1}{1+0.35T_i} \cdot \text{Timefast} = \frac{d_i}{v_{\text{fast}}}, \text{Time}_{\text{slow}} = \frac{d_i}{v_{\text{slow}}} \)

\[ t_i = \sum_{\tau = \text{Timefast}}^{\text{Timel slow}} T_i (1 - F) T_i - \text{Timefast} \cdot Z \]

(24)

where \( F = \frac{1}{1+0.35T_i} \cdot \text{Timefast} = \frac{d_i}{v_{\text{fast}}}, \text{Time}_{\text{slow}} = \frac{d_i}{v_{\text{slow}}} \). \( \text{Time}_{\text{fast}} (\text{Time}_{\text{slow}}) \) is the travel time of fastest (slowest) vehicle between intersections \( i \) and \( i+1 \) in an outbound (inbound) path.

Consequently, the RMPPM2 is written as the follows:

\[ \text{RMPPM2} \quad \text{Max} \quad \sum_p (\phi_p b_p) + \sum_p (\phi_p b_p) \]

s.t. Eqs. (2) – (14), (18), (21) – (24)

3 NUMERICAL EXPERIMENTS

3.1 Empirical study

Areal-world application is conducted on the proposed models. The actual flow data of an arterial system containing a highway ramp and surface signalized intersections in Chubei City in Taiwan are analysed. Figure 1 shows the topology for the underlying arterial system. The traffic data were collected during 17:00 p.m. – 21:00 p.m. in April 13th, 2013. Five critical paths are chosen for evaluation in accordance with the traffic data. Path 1 contains the traffic flow from the northbound off-ramp through the major arterial; paths 2 and 3 pass through the major arterial in opposite directions; and paths 4 and 5 are from minor legs of the surface signalized intersections to the major arterial. We mark the three intersections, from right to left, as 1, 2 and 3,
respectively. Also, paths 1 and 2 are outbound paths, and paths 3, 4, and 5 are inbound paths.

### 3.2. Numerical implementations

For numerical implementations, both problem solving and traffic simulations for performance evaluations are carried out. For problem solving, a C++ program is coded for connecting the CPLEX solver for obtaining a feasible timing plan for the proposed models introduced in Section 2. Obtained signal timing plans then serve as the input to the traffic software integrated system (TSIS) for random simulations. A total of 500 independent replications are performed and output the associated performance measures.

On-going timing plans as well as those suggested in Yang et al. are used for comparisons. Designs of phases at each intersection of the two plans are given in Table 2 and Table 3.

![Chubei Network](image)

**Table 2. On-going Timing Plan Design**

<table>
<thead>
<tr>
<th>Intersection</th>
<th>Phase 1</th>
<th>Phase 2</th>
<th>Phase 3</th>
<th>Phase 4</th>
</tr>
</thead>
<tbody>
<tr>
<td>Intersection 1</td>
<td><img src="image" alt="Phase 1" /></td>
<td><img src="image" alt="Phase 2" /></td>
<td><img src="image" alt="Phase 3" /></td>
<td><img src="image" alt="Phase 4" /></td>
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<tr>
<td>Intersection 2</td>
<td><img src="image" alt="Phase 1" /></td>
<td><img src="image" alt="Phase 2" /></td>
<td><img src="image" alt="Phase 3" /></td>
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<tr>
<td>Intersection 3</td>
<td><img src="image" alt="Phase 1" /></td>
<td><img src="image" alt="Phase 2" /></td>
<td><img src="image" alt="Phase 3" /></td>
<td><img src="image" alt="Phase 4" /></td>
</tr>
</tbody>
</table>

**Table 3. Yang’s Timing Plan Design**

<table>
<thead>
<tr>
<th>Yang’s plan</th>
<th>Phase 1</th>
<th>Phase 2</th>
<th>Phase 3</th>
<th>Phase 4</th>
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<tbody>
<tr>
<td>Intersection 1</td>
<td><img src="image" alt="Phase 1" /></td>
<td><img src="image" alt="Phase 2" /></td>
<td><img src="image" alt="Phase 3" /></td>
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<tr>
<td>Intersection 3</td>
<td><img src="image" alt="Phase 1" /></td>
<td><img src="image" alt="Phase 2" /></td>
<td><img src="image" alt="Phase 3" /></td>
<td><img src="image" alt="Phase 4" /></td>
</tr>
</tbody>
</table>

Numerical results are summarized in Table 4 and Table 5. The revised results (Plan b, Plan c, Plan y and Plan z) are derived from solving our models. Note that both the phase sequences and cycle lengths differ from the original timing plans (Plan a and Plan x).

From Table 4, we see that the cycle length suggested by the proposed model is now longer than the original timing plan. From the timing plan in Plan b, we observe that the lengths of the phase 1 at intersections 1 and 2 have increased. In particular, this allows more traffic on the major arterial in outbound directions (path 1 and path 2). On the other hand, from the result of Plan c, the cycle length decreases in Plan a, while it increases in Plan b. Also, comparing Plan b and Plan c, the ratio of the phase 1 decreases while the ratio of phase 2 increases. This suggests that sacrificing the benefit of outbound paths can improve that of the inbound paths.

From Table 5, as for the plan suggested by Yang et al., we can see that comparing the original plan (Plan x), the cycle length decreases both in the results of RMPPM 1 (Plan y) and RMPPM 2 (Plan z). For intersection 3 with high right-turn traffic, the model result suggests a longer length of that phase so that the right-turn traffic can dissipate more therein. This can be observed from the results that the ratio of phase 4 at intersection 3 increases. The cycle length of Plan z is longer than Plan y, but all the phase ratios are closely the same.

### 3.3. Performance evaluations

To evaluate the system performance under different signal timing plans, we adopt the total control delay per minute in the network as the performance measure. Figure 2 and Figure 3 show the results for the timing plan containing in Table 4 and Table 5, respectively.

Colored lines in Figure 2, from the top to the bottom, correspond to the total control delay per minute of plans a, b, and c, respectively. It is apparent from Figure 2 that Plan c outperforms the rest plans with respect to the on-going timing plan. Compared to the original signal (Plan a), the improvement with Plan c is around 44.39% in terms of total control delay per minute of the network; and around 15.59% compared to plan b. It can be noticed that Plan c, as a matter of fact, comes with the shortest cycle length. We infer that while the cycle length becomes longer, the phase lengths become longer. In this case, at the intersection 1, the left-turning flow from the westbound will form a queue if the red time is too long, preventing the eastbound left-turning traffic flow at intersection 2 from dissipating.

Lines on Figure 3 are the total control delay per minute of plans x, y, and z, respectively. Results show that Plan y is the best amongst the rest. The improvement is around 59.57% of delay compared to Plan x and 13.12% of delay compared to Plan z.

We further compare the performance of each path under the Plan a to Plan c and plan y. This is because Plans c and y are respectively the best alternatives derived from solving the RMPPM 1 and RMPPM 2. When we compare Plan c to Plan a, the improvements of the paths are around 20-52% on average, resulting basically from the improvements on the arterial paths (Path 2 and 3). In terms of delay, the improvements are around 37-49%. Yet, when compared to Plan y, even though the performance of Path 2 and 3 has improved around 17%-
65%, the performance of the minor paths is less satisfactory, being around -7%-33%.

Table 4. Model Results For On-going Timing Plan

<table>
<thead>
<tr>
<th>Plan Number</th>
<th>Timing Plan</th>
<th>a</th>
<th>b</th>
<th>c</th>
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<tbody>
<tr>
<td>#</td>
<td>Offset</td>
<td>Phase Num</td>
<td>Phase Length</td>
<td>Offset</td>
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<td>56</td>
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<td>52</td>
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<td>Cycle Length</td>
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Table 5. Model Results Timing Plan Suggested in Yang et al.11

<table>
<thead>
<tr>
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Lastly, we compare Plan c to Plan y. From the perspective of path performance, Plan c is around 10% better than Plan y with respect to Paths 1 and 5. Yet, on the other hand, Plan y yields better results on Path 3. As to Paths 2 and 4, Plan y is better. Despite this fact, Plan c is the best alternative in terms of the aggregate network delay, possibly due to the lack of efficiency in the turning flow at intersection 3 under Plan y.

Conclusions

In this paper, extensions of the signal synchronization model proposed in Yang et al.11 are given by letting the ratios of phases become variable, and by incorporating the traffic flow dispersion module for adjusting the travel times. Numerical evidences suggest a total improvement of around 44.39% and 59.57% with on-going timing plan and those suggested by Yang et al.11, respectively, in terms of the total control delay per minute of the entire network. We observe that in this experiment, the results of RMPPM 2 are not always better than that of RMPPM 1. This may be due to interference of the paths that we have not considered in the experiment - such as the path flow from the northbound of intersection 2 and the left-turning flow at intersection 2 - or the red time is too longer to remove the queue in each cycle and keep the progression.

Comparisons on the performance of each path under different plans are carried out as well. Results show that compared to the on-going timing plan (Plan a), with Plan c, the total control delay of each path can be improved around 20% to 52%; with Plan y, the total control delay of paths mainly in the major, such as path 2 and path 3, will be improved around 17% to 65%. But when it comes to paths through the branches, the results of our model have a smaller contribution for the total control delay of them, due to the difference of the signal design.

As of this moment, discussions of the signal synchronization problem still are limited by assuming that the design of the phases comprising a cycle is pre-defined. A potential future research direction resides in the optimal design of phases for signalized intersections. A proper design of phases can certain help improve the LoS of both the underlying signalized intersections and the entire network associated.

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