Analysis heat transfer in engineering barriers used FEM and experimental method

Dariusz Andrzejewski¹*, and Mariusz Prazmowski¹

¹Opole University of Technology, Faculty of Mechanical Engineering, 5 Mikołajczyka St., Opole, Poland

Abstract. Purpose of the calculations is to determine the temperature field at various points in the area in question. Estimate the losses of heat given off by the analysed structures to the environment. Numerical algorithm based on the Finite Element Method for steady flow of heat and areas of heterogeneous. To analyse was used windows with double-glazed unit made PCV with different option gasses and glasses. Verification the simulation which used numerical procedures by experimental method.

1 Introduction

To analysis we have an engineering barrier (windows panel set double glazed resized specially for experimental check in heater chamber with different glasses and used gases) which will be realised algorithm numerical simulation. Besides checking the optimally distances for provide the best insulation between double glazed set has been proven impact on the size panel set for thermal insulation. Specify the temperature field in the distinguished points of the area in question arising from the way the geometrical discretization of the continuum to estimate the losses of heat given off by the design of this analysed. To solve a issues was applicable finite element method (FEM) in variant published in the[1].To finally calculation was used author program to automatic generation net differential where finally equations was develop iterative method Gauss-Seidel [2,3].

We try find optimum distance between two set of glasses in window panel for smallest heat transfer coefficient, use correct glass, gasses and material for construction and design in order to improve save energy used author program and compare to commercial program “Fluent”. As well opportunity to use the internal heating plates of glass to eliminate thermal bridge causing condensation of the water at the bottom of the glass. Opportunity to use specific system of cooling the glass to blocked move the heat from the outside to the inside.

2 Material and methods

2.1 Mathematics process

In mathematics problem it’s described differential equations [2-4]:

*Corresponding author: d.andrzejewski@po.opole.pl
\[
\frac{\partial}{\partial x_1} \left[ \lambda_e \left( \frac{\partial T_e}{\partial x_1} \right) \right] + \frac{\partial}{\partial x_2} \left[ \lambda_e \left( \frac{\partial T_e}{\partial x_2} \right) \right] = 0
\]  
(1)

\( \lambda_e \)-thermal conductivity  
\( T_e \)-temperature field in area  

For testing calculation checked effective value for numerical calculation. Any convection in “empty” area made effective coefficient instead real thermal conductivity. 

Equations for calculation:

\[
\frac{\partial}{\partial x_1} \left[ \lambda_e \left( \frac{\partial T_e}{\partial x_1} \right) \right] + \frac{\partial}{\partial x_2} \left[ \lambda_e \left( \frac{\partial T_e}{\partial x_2} \right) \right] = 0
\]  
(2)

Adopted boundary conditions Robin:

\[ x \in \Gamma_z: -\lambda_e \frac{\partial T_e}{\partial n} = \alpha_z [T_e - T_z] \text{ and } x \in \Gamma_w: -\lambda_e \frac{\partial T_e}{\partial n} = \alpha_w [T_e - T_w] \]  
(3)

\( w \)- area inside, \( z \)-area outside, \( \alpha \)- heat transfer coefficient \( \partial / \partial n \)- derivative normal to the edge of the area.  

At the contact surface there are continuity conditions [4, 5]:

\[ x \in \Gamma_{e, \hat{e}}: -\lambda_{e, \hat{e}} \frac{\partial T_{e, \hat{e}}}{\partial n} = -\lambda_{e, \hat{e}} \frac{\partial T_{e, \hat{e}}}{\partial n}, T_e = T_{\hat{e}} \]  
(4)

\( e, \hat{e} \)- ideal contact surface, for surface no flux conditions

**Fig.1.** Analysing area: 1-glasses, 3-distance block, 4-gasket, 5-PVC profile, 6-aluminium strengthening, 7-Gasket connector, 8,11- air chamber, 10- drainage hole, 12-wall connector [6].

**Fig.2.** Consideration area and matrix identification [6,13-16].
2.2 Numerical model

Consider the area was covered with a net differential (Fig. 3).

![Image of a five-point star net]

**Fig. 3.** Five points star net.

Approximation equations shows the relation between central node and neighbor nodes.

\[
\frac{T_{i+1,j} - T_{i,j}}{R_{i+1,j}} \Phi_{i+1,j} + \frac{T_{i-1,j} - T_{i,j}}{R_{i-1,j}} \Phi_{i-1,j} + \frac{T_{i,j-1} - T_{i,j}}{R_{i,j-1}} \Phi_{i,j-1} + \frac{T_{i,j+1} - T_{i,j}}{R_{i,j+1}} \Phi_{i,j+1} = 0
\]  

(5)

**R-** resistance to heat flow, \(\Phi = \frac{1}{k}\)

\[
A_0 T_{i,j} - A_1 T_{i+1,j} - A_2 T_{i-1,j} - A_3 T_{i,j-1} - A_4 T_{i,j+1} = 0
\]  

(6)

\[
T_{ij} = \frac{A_1}{A_0} T_{i+1,j} - \frac{A_2}{A_0} T_{i-1,j} - \frac{A_3}{A_0} T_{i,j-1} - \frac{A_4}{A_0} T_{i,j+1}
\]  

(7)

2.3 Numerical realization

The area was covered with net it has steps \(h=0.001\text{m}\) [13,14].

Area which was considered has got 10576 points. The matrix type integer (Fig.2).

Window size: S 1465mm x H 2195mm, glass 4mm,distance between glazing: 12-18mm,\(T_{\text{inside}}=20^\circ\text{C}\), \(T_{\text{outside}}= -20, -15, -10, -5\,\text{.}0\) (in subsequent calculations),\(\sigma_w=8.1\,\text{W/m}^2\text{K}\), \(\alpha_e=23\,\text{W/m}^2\text{K}, \lambda_{zz1}=0.744\,\text{W/mK}, \lambda_{zz2}=1.338\,\text{W/mK}.

Numerical realization was done used special for this prepared author program.

3 Results and discussions

Results simulation show parameters \(k\) and \(q\) for different set points temperatures in term of \(-20^\circ\text{C}\) to \(0^\circ\text{C}\). When we take into account \(\lambda_{er}\) results was increase about 57.5% what good correlation to real experimental results.

**Table 1.** Numerical simulation results.

<table>
<thead>
<tr>
<th>N°</th>
<th>(T_{z\text{(outside)}}) [C°]</th>
<th>(T_{w\text{(inside)}}) [C°]</th>
<th>q [W/m²]</th>
<th>k [W/m²K]</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>-20</td>
<td>20</td>
<td>48.21</td>
<td>1.205</td>
</tr>
<tr>
<td>2</td>
<td>-10</td>
<td>20</td>
<td>36.17</td>
<td>1.206</td>
</tr>
<tr>
<td>3</td>
<td>0</td>
<td>20</td>
<td>24.12</td>
<td>1.206</td>
</tr>
</tbody>
</table>

When changed for effective conductivity coefficient (\(\lambda_{er}=\lambda_{zz}+\lambda_{zz2}\))

<table>
<thead>
<tr>
<th>N°</th>
<th>(T_{z\text{(outside)}}) [C°]</th>
<th>(T_{w\text{(inside)}}) [C°]</th>
<th>q [W/m²]</th>
<th>k [W/m²K]</th>
</tr>
</thead>
<tbody>
<tr>
<td>4</td>
<td>-20</td>
<td>20</td>
<td>75.46</td>
<td>1.89</td>
</tr>
<tr>
<td>5</td>
<td>-10</td>
<td>20</td>
<td>56.60</td>
<td>1.89</td>
</tr>
<tr>
<td>6</td>
<td>0</td>
<td>20</td>
<td>37.72</td>
<td>1.89</td>
</tr>
</tbody>
</table>

Graphical presentation simulation which result show in Table 1 (Author program).
Graphical presentation show areas when different colours are assigned to a specific temperature. Area in specific colour show distribution temperature for interpretation when we have place which must be structural remodel.

**Table 2.** Show termoalsolation optimum distance between glasses, size affected heat transfer coefficient and gases have got changes for result [7].

<table>
<thead>
<tr>
<th>№</th>
<th>Distance between glasses [mm]</th>
<th>Panel H[mm]</th>
<th>gas</th>
<th>$T_{_\text{outside}}$[°C]</th>
<th>glass</th>
<th>Heat lost[J]</th>
<th>k[W/m²K]</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>15</td>
<td>1400</td>
<td>Air</td>
<td>-20</td>
<td>quartz</td>
<td>92</td>
<td>1.64</td>
</tr>
<tr>
<td>2</td>
<td>15</td>
<td>1400</td>
<td>Argon</td>
<td>-20</td>
<td>float</td>
<td>67.7</td>
<td>1.21</td>
</tr>
<tr>
<td>3</td>
<td>15</td>
<td>1400</td>
<td>Air</td>
<td>-20</td>
<td>float</td>
<td>83</td>
<td>1.48</td>
</tr>
<tr>
<td>4</td>
<td>15</td>
<td>1400</td>
<td>Air</td>
<td>-10</td>
<td>float</td>
<td>61.4</td>
<td>1.46</td>
</tr>
<tr>
<td>5</td>
<td>15</td>
<td>1400</td>
<td>Air</td>
<td>0</td>
<td>float</td>
<td>37.5</td>
<td>1.34</td>
</tr>
<tr>
<td>6</td>
<td>18</td>
<td>1400</td>
<td>Air</td>
<td>-20</td>
<td>float</td>
<td>83.2</td>
<td>1.49</td>
</tr>
<tr>
<td>7</td>
<td>12</td>
<td>1400</td>
<td>Air</td>
<td>-20</td>
<td>float</td>
<td>90.2</td>
<td>1.61</td>
</tr>
<tr>
<td>3'</td>
<td>15</td>
<td>1400</td>
<td>Air</td>
<td>-20</td>
<td>float</td>
<td>83</td>
<td>1.48</td>
</tr>
<tr>
<td>8</td>
<td>15</td>
<td>2600</td>
<td>Air</td>
<td>-20</td>
<td>float</td>
<td>154.1</td>
<td>1.48</td>
</tr>
</tbody>
</table>

In table 2 we have results part of interesting simulations which shows optimal distance between glasses (15 mm) which guarantee maximum isolation. When we increases or decreases the distance between glasses, k changes what means heat transfer have to high level and we lost optimum termoalsolation. Similar situation we have when we use quartz glass not float glass. Heat transfer coefficient increase about 11% when we have in windows quartz glass. If we use different gases not air, example Argon or Krypton heat transfer coefficient ensure better termoalsolation about 22%. When we would like the same
result when we used Argon or Krypton we must between glasses used “air vacuum”.

Interesting situation we have when we used higher window panel and compare to standard panel.

Heat transfer coefficient it is constant. Meaning highest panel set not decrease termiosilation.

We were check different construction as well for find better opportunity. Double glasses window which have between glasses on the middle spectroselective foil (in PVD technology was sputtered metal oxides). Results: k =1 W/m²K. Radiation UV=0. Short IR only 6%. Because this foil stopped radiation longer than 380nm flowers don’t have light to life!

As well shadow coefficient increased to 0.66, resulting for this we have better protection against overheating. Visibility 88%.

Graphical presentation simulation which result show in Table 2.

Convection which we see on the Fig. 8. and Fig. 10 was simulation done in commercial program fluent 5 shows Bernard cells. Fig. 8, 9, 11,12 shows graphical presentation results from Table 2.

Fig. 8. Set of glass for optimality distance between glazed [8].

Fig. 9. Optimum distance between glasses.

Fig. 10. We have Bernard cells characteristic for free convection in close space between glasses. [7, 9].

Fig. 11. Affect heat transfer coefficient in glass panel used different gases [10].

Fig. 12. Affect heat transfer coefficient in glass panel used different glass [10].

4 Experimental study

Results measured in heating chamber have a very good correlation with simulation results. Experimental verification helped confirm the correctness of the tests simulation.

Differences of 3% between the method of calculation and experimental confirms that the application of the calculation method is justified in order to search for the optimal
design solution for partitions heat.

Windows samples were tested in a heating chamber [13].

![Diagram of heating chamber scheme](Fig. 13. Heating chamber scheme [11, 12].)

Parameters for samples: \( T_1 = 20^\circ C \), \( T_2 = -20^\circ C \), \( h_e = 23 \text{ W/m}^2\text{K} \), \( h_i = 8 \text{ W/m}^2\text{K} \)

<table>
<thead>
<tr>
<th>Set of glass in panel</th>
<th>Gas between set of glasses</th>
<th>( k ) [W/m(^2)K]</th>
</tr>
</thead>
<tbody>
<tr>
<td>4-15-4 float</td>
<td>air</td>
<td>1.49</td>
</tr>
<tr>
<td>4-15-4 quartz</td>
<td>air</td>
<td>1.67</td>
</tr>
<tr>
<td>4-15-4 float</td>
<td>air</td>
<td>1.62</td>
</tr>
<tr>
<td>4-15-4 float</td>
<td>air</td>
<td>1.51</td>
</tr>
<tr>
<td>4-15-4 float</td>
<td>argon</td>
<td>1.23</td>
</tr>
</tbody>
</table>

### 5 Conclusions

1. Between both methods we have a good correlation simulation where for set 4-15-4 float was \( k = 1.48 \text{ W/m}^2\text{K} \), used argon \( k = 1.21 \text{ W/m}^2\text{K} \) and for quartz \( k = 1.64 \text{ W/m}^2\text{K} \) and experimental where was 4-15-4 float was \( k = 1.52 \text{ W/m}^2\text{K} \), used argon \( k = 1.23 \text{ W/m}^2\text{K} \) and for quartz \( k = 1.67 \text{ W/m}^2\text{K} \) means only 3% difference, this allow the use of simulation methods in research application.

2. We found optimum distance between glasses in window panel for the best isolation, it is 15mm between glasses in window panel. If we try increase distance between glasses slowly increases \( k \) (from \( k = 1.48 \text{ W/m}^2\text{K} \) for 15mm to \( k = 1.49 \text{ W/m}^2\text{K} \) for 18mm), if we try decrease distance much faster changed \( k \) (from \( k = 1.48 \text{ W/m}^2\text{K} \) for 15mm to \( k = 1.61 \text{ W/m}^2\text{K} \) for 12mm).

3. Used different gasses between glasses changed termoisolations in set of window. Argon changed approximately 26% heat transfer coefficient from \( k = 1.48 \text{ W/m}^2\text{K} \)(air) tok=1.21 W/m\(^2\)K (argon)

4. Different kind of glass affect heat transfer coefficient too. Set 4-15-4 float glass with air
k=1.48 W/m²K but the same set with air for quartz glass k=1.64 W/m²K this is different more than 9%.
5. Possibility used electric wire to heat up inside glass for better isolation and reduce heater bridge on the button for considered size window 160 W-300 W according to temperature outside building.
6. Alternative connection to solar panel on sun water panel to heat up.
7. Possibility connect to geothermal heat pomp for heat up frame and glass or in summer cool down to 12.2°C and will be works like small air-condition.

References
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