

# DEVELOPMENT OF THE MATHEMATICAL MODEL OF DIESEL FUEL CATALYTIC DEWAXING PROCESS TAKING INTO ACCOUNT FACTORS OF NONSTATIONARITY

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**Abstract.** The paper describes the results of mathematical modelling of diesel fuel catalytic dewaxing process, performed taking into account the factors of process nonstationarity driven by changes in process technological parameters, feedstock composition and catalyst deactivation. The error of hydrocarbon contents calculation via the use of the developed model does not exceed 1.6 wt.%. This makes it possible to apply the model for solution to optimization and forecasting problems occurred in catalytic systems under industrial conditions. It was shown through the model calculation that temperature in the dewaxing reactor without catalyst deactivation is lower by 19 °C than actual and catalyst deactivation degree accounts for 32 %.

## 1 Introduction

Production of various grades of diesel fuels according to the EURO-5 standard is a complex multistage chemical process scheme, which includes the stages of catalytic refining of wide diesel fraction. This fraction contains such hydrocarbon groups as paraffins, naphthenes, aromatic and olefins. One more stage of production implies the process of rectification and separation of the obtained product. These processes are operated in a system of adjacent and interconnected reactor apparatus. The feedstock of the process is a mixture of diesel fractions and atmospheric gasoil.

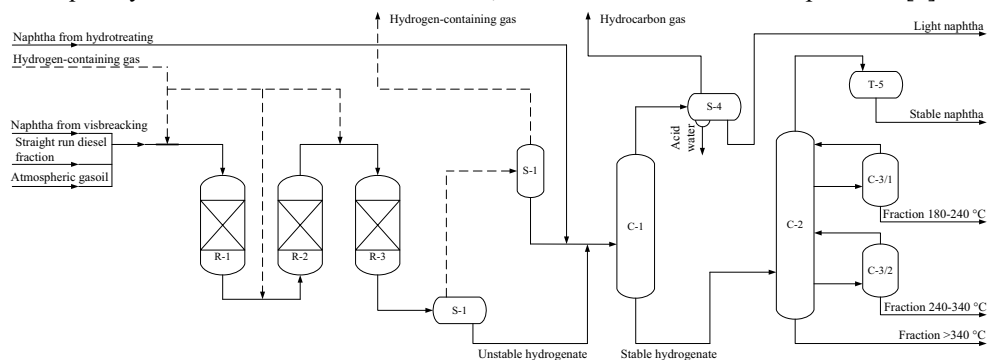
The process is aimed to produce a stable naphtha, diesel fraction with improved low-temperature properties, and residue with a boiling point of above 340 degrees of Celsius [1].

The process occurs in three reactors. The first two reactors are hydrotreating reactors with a nickel-molibdenum catalyst, the third one is a dewaxing reactor with nickel catalyst. Process temperature is 350–400 °C. The reactions of hydrocracking, hydroisomerization, hydrogenation of unsaturated hydrocarbons, hydrogenation of mercaptanes followed by hydrogen sulfide formation, aromatization and coke formation take place [2].

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After reactor section the products enters the stabilization column, where the light hydrocarbons, hydrogen sulfide and water are eliminated. The stable hydrogenate subsequently flows to the rectification section, where it is fractionated into products [3].



**Fig. 1.** Technological scheme of hydrodewaxing plant for production of diesel fuels  
 R-1, R-2 – hydrotreating reactors; R-3 – hydrodewaxing reactor; S-1 – high pressure separator; S-2 – low pressure separator; C-1 – stabilization column; C-2 – rectification column; S-3/1, S-3/2 – strippers; RT-5 – reflux tank.

## 2 Materials and methods

The method of mathematical modelling is widely used to study, improve, optimize and forecast the processes of petroleum refining industry [4-14].

The main task of the industrial process realization to be solved is sustaining high product yield with required quality. This is possible when developing the optimal technology of the catalyst operation which would allow using the catalyst resource as high as possible, following the required quality and quantity of the product.

To meet this challenge, the method of mathematical modelling was used. The model was developed on the basis of account for thermodynamic and kinetic laws of the process, factors of nonstationarity caused by variability of technological regime, feedstock composition and catalyst deactivation.

Accounting the thermodynamic and kinetic laws of the process allows developing the model sensitive to change in technological parameters and feedstock composition. This provides using the model for forecasting feedstock conversion degree, product composition and yield, as well as for process optimization within valid industrial technological conditions (temperature 335 – 365 °C, feedstock flow rate 295 – 325 m<sup>3</sup>/h, hydrogen-containing gas flow rate 35000 – 65000 m<sup>3</sup>/h).

The experimental data from the industrial unit has been used as the initial data for modelling. These data included operating conditions in a wide range of changing feed flow rate, temperature, HBG (hydrogen bearing gas) flow rate and its composition, and also the feed and the product content with a range of hydrocarbon group concentrations.

Mathematical model considering deactivation:

$$\begin{cases} G \cdot \frac{\partial C_i}{\partial z} + G \cdot \frac{\partial C_i}{\partial V} = \sum_{j=1}^m a_j \cdot W_j \\ G \cdot \frac{\partial T}{\partial z} + G \cdot \frac{\partial T}{\partial V} = \frac{1}{\rho \cdot C_p} \sum_{j=1}^m Q_j \cdot a_j \cdot W_j \end{cases}$$

Initial conditions:

$$z = 0: C_i = C_{i,0}; T = T_0;$$

$$V = 0: C_i = C_{i,0}; T = T_0,$$

where  $z$  is the volume of the refined feedstock from the moment of fresh catalyst loading,  $m^3$ ;  $G$  is the feed flow rate,  $m^3/h$ ;  $z = G \cdot t$  ( $t$  is catalyst operating time from the moment of fresh catalyst loading, h);  $C_i$  is the concentration of  $i$ -component, mole/l;  $V$  is a catalyst bed volume,  $m^3$ ;  $a_j$  is a catalyst activity in  $j^{\text{th}}$  reaction;  $\rho$  is mixture density,  $kg/m^3$ ;  $C_p^m$  is specific heat capacity of the mixture,  $J/(kg \cdot K)$ ;  $Q_j$  is heat effect of  $j^{\text{th}}$  reaction, J/mole;  $T$  is a temperature, K;  $W_j$  is a  $j^{\text{th}}$  reaction rate, mole/(l\*s);  $m$  is number of reactions.

This model takes into account catalyst deactivation. Catalyst activity can be determined as a proportion of reaction rate constant at any time to the reaction rate constant at the initial moment of the time when the fresh catalyst had been charged:

$$a_j = \frac{k_{j,t}}{k_{j,0}}$$

where  $k_{j,0}$  is  $j^{\text{th}}$  reaction rate constant at the initial moment of time (with the fresh catalyst);  $k_{j,t}$  is  $j^{\text{th}}$  reaction rate constant at the current moment of time.

$$a_j = A_j \cdot e^{-\alpha_j C_c}$$

where  $A_j$ ,  $\alpha_j$  are the deactivation coefficients;  $C_c$  is coke concentration, % wt.

Deactivation coefficient includes the deactivation of metal and acid centers:

$$a_j = a_{a,j} + a_{m,j}$$

where  $a_a$  is the catalyst acid center activity;  $a_m$  is the catalyst metal center activity.

### 3 Results

Model adequacy examination was conducted by comparing the calculated data with experimental data from the industrial unit.

It is shown that the model is suitable for the process and can be applied for identification of the process laws, forecast calculations conduction and optimization.

**Table 1.** Calculated and experimental data comparison

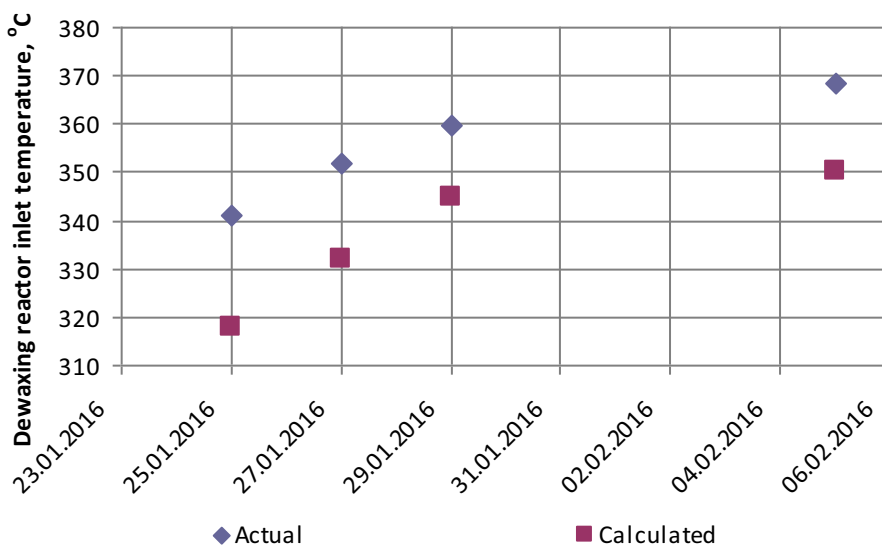
Product (experimental), % wt.	Product (calculation), % wt.	Error (absolute), % wt.
n-paraffins C <sub>10</sub> –C <sub>27</sub>		
10.17	11.18	1.01
10.08	10.19	0.11
9.32	9.48	0.16
i-paraffins		
26.46	26.40	0.06
24.66	24.82	0.16
23.14	25.67	2.53
Olefins		
1.74	1.99	0.25
2.63	2.58	0.05
2.25	2.35	0.10
MNA		
20.53	20.06	0.47
19.90	20.09	0.19
19.30	19.73	0.43

The abbreviation in Table 1: MNA is monoaromatic compounds.

Computations via the use of the model showed that temperature inside the dewaxing reactor without catalyst deactivation is on the average lower than actual by 19 °C, considering the required product yield of the same quality concerning cold filter plugging point (CFPP) (Table 2).

**Table 2.** Computation of the deactivation compensating temperature

Date	Yield of fraction 240-340 (DF), %	CFPP, °C	T <sub>in</sub> R-3 (actual), °C	T <sub>in</sub> R-3 (comp.), °C	ΔT, °C
25.01.2016	41.4	-34	341	318	23
27.01.2016	41.8	-37	352	332	20
29.01.2016	41.5	-44	360	345	15
05.02.2016	43.0	-41	369	350	19



**Fig. 2.** Computation of the temperature which compensate catalyst deactivation

The level of relative catalyst activity at the cycle end (2016 year) equals to [15]:

$$Akt = \frac{\Delta - \Delta T}{\Delta} = \frac{60 - 19}{60} = 0.68$$

Where Δ is a largest possible temperature range in the process (330 – 390 oC); ΔT is a temperature that compensates deactivation. The activity of fresh catalyst equals to 1.

To sum up, deactivation of the catalyst in the period of operation accounts for 32%.

## 4 Conclusion

The developed mathematical model of catalytic dewaxing process is valid for description of the real process since the absolute calculation error of hydrocarbon contents in the product does not exceed 1.16 wt.%.

Accounting for factors of nonstationarity, caused by variability of technological regime, feedstock composition and catalyst deactivation, allows applying the developed model for solution to problems of industrial catalysts operation.

It was shown through the model calculation that temperature in the dewaxing reactor without catalyst deactivation is lower by 19 °C than actual and catalyst deactivation degree accounts for 32 %.

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