A model for the grasping analysis of an underactuated finger driven by unextensible tendon

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Abstract. A grasping analysis is presented of an underactuated finger driven by unextensible tendon. The finger itself is one of those of a mechanical prosthesis that was principally conceived as human prosthesis. After a brief description of the whole system constituted by the mechanical hand, the model to predict the behavior of the finger during the grasping is presented; then some examples of grasping are presented. The model can be useful for both the under-actuated finger design and for the prediction of the capabilities of the whole hand.

1 Introduction

A number of Authors have investigated on mechanical grasping devices and hand prosthesis in particular [1-6]. These devices are based on mechanical systems using a number of motors [ 7-10 ] or on self-adapting devices using a single motor [11-13].

Among the later, the authors of this contribution developed a new mechanical hand (Federica mechanical hand) based on a self-adapting patented scheme (patent n. 0001415546 and n. 102015000059873, the latter pending) [14-18] that is briefly described in figure 1. In the figure a prototype is shown and a CAD design showing the working principle is also reported.

The hand is composed by five fingers, shown in figure 2, actuated by a single motor by means of a pulley system in cascade, which automatically distributes the tendon displacement to the phalanges. Each finger consists of three elements, representing respectively the distal, medial and proximal phalanges, joined by hinges, and activated by a single inelastic tendon. The grasp of an object of any shape is obtained by operating the main inelastic tendon, which, through the pulley system, distributes the force among the various fingers, and generates the closure of each finger according to the resistance offered by the object to be grasped in the contact points.

In this contribution, the authors focused themselves on the study of the grasping of the single finger in order to optimize the finger behavior during the grasping itself.

Some examples of contact between the finger phalanxes and a solid surface having a defined geometrical shape are considered.

The contact between the finger and a surface has been studied using the Simulink library called SimMechanics contact forces downloaded from the Mathworks. The library provides different blocks according to the type of surface to be treated. We focused mainly on two blocks, the "sphere to plane" and the "sphere to tube". The object of the study is the contact between the proximal phalanges, medial and distal and a sphere and, in addition, the contact between the tip of the finger shown schematically with a cylindrical surface and a sphere.

Figure 1. The underactuated, self-adapting mechanical hand.
2 The contact between surfaces

The contact between the finger and a surface has been studied using the Simulink library called SimMechanics contact forces downloaded from the Mathworks. The library provides different blocks according to the type of surface to be treated. We focused mainly on two blocks, the "sphere to plane" and the "sphere to tube". The object of the study is the contact between the proximal phalanges, medial and distal and a surface and, in addition, the contact between the tip of the finger shown schematically with a cylindrical surface and a sphere.

The contact between two bodies was simulated with a force applied only along the direction of penetration of the two bodies. In figure 5 this force is shown as $F_n$, and it acts on the plane and on the sphere in the opposite direction. In the contact model, also the friction force is included; it acts as a tangential force in the contact point on both bodies. In figure 3 the friction force is shown as $F_t$.

The normal force $F_n$ acts by opposing the penetration of the two bodies and the damping is zero when the penetration decreases.

$$F_n = \begin{cases} k \cdot Z_{\text{penetration}} + b \cdot v_{\text{penetration}} & \text{if } Z_{\text{penetration}} > 0, v_{\text{penetration}} > 0 \vspace{2mm} \\
0 & \text{if } Z_{\text{penetration}} > 0, v_{\text{penetration}} < 0 \\
-k Z_{\text{penetration}} - b v_{\text{penetration}} & \text{if } Z_{\text{penetration}} < 0 \end{cases} \quad (1)$$

Where $Z_{\text{penetration}}$ is the penetration between the two bodies, $v_{\text{penetration}}$ is the velocity of penetration, $k$ is the contact stiffness and $b$ is the contact damping.

The friction force $F_t$ is the product of normal force and a coefficient of friction that is a function of the relative velocity at the contact point.

Examples of the tool to study the contact between a sphere and a plane or between a sphere and a tube are reported in fig. 4.

By using the original blocks of SimMechanics contact forces library we observed that it is not possible to model the edge effect between finger and ball. This circumstance is a drawback because many contact intermediate positions, i.e. those in which the ball is located between two fingers, are not correctly handled (a finger can penetrate the sphere).

In order to make the appropriate corrections we considered a simpler system constituted by a plane and a sphere; in fig. 5 mentioned drawback can be observed.
The main changes made to take account of the contact between the ball and the edge of the plan include the evaluation of the contact condition by introducing the following quantities:

\[ dx_c = |x| - \frac{\text{plane_length} x}{\sqrt{2}} \]  

\[ dy_c = |y| - \frac{\text{plane_length}}{2} \]  

\[ r_u = \sqrt{\text{sphere_rad}^2 - (dx_c^2 + dy_c^2)} \]  

Representing the distance of the sphere center from the edge of the plane, like it is possible to see in figure 6.

Calculating the forces acting on the ball we reported the components of the normal force in the plane reference system according to the following equations:

\[ F_x = \frac{r_u}{\sqrt{dx_c^2 + dy_c^2}} \cdot dx_c \]  

\[ F_y = \frac{r_u}{\sqrt{dx_c^2 + dy_c^2}} \cdot dy_c \]  

This in order to permit a correct impact between ball and plane and an eventual fall from the plane.

The sign of the moments of the forces acting on the sphere was changed in order to permit the correct rotation (clockwise or counter clockwise) depending on the contact of the sphere with the edge of the plane.

Similar expedients were adopted for the contact between ball and tube. In Figure 7 a wrong contact (up) and a wrong contact between ball and tube are shown.

In this section some of the simulation results are reported.

### 3.1 The contact between finger and sphere

The blocks of the library SimMechanics Contact Forces, originally forecast in the model Federica hand, involve a situation like the one shown in figure 8, where penetration occurs between finger and ball.
Thanks to the changes seen in the previous paragraphs, it is possible to evaluate all the intermediate positions; an example of this result is shown in figure 9.

For each of the fingers, four blocks sphere to plane were used in order to simulate the contact between the inner surfaces of the phalanxes and the sphere and between the palm of the hand and the sphere and another block sphere to tube for the contact between the fingertip and the sphere.

In the simulations we assumed to grab spheres having different sizes that can be fixed on the palm in a specific position (using the weld joint block of SimMechanics) or can be free to move on the palm. The latter situation is supposed to be a result of an impact between the sphere and a finger phalanx before the sphere was grabbed; this was obtained by using the bushing joint block. The output variables of each contact block are analyzed in a subsystem called Grasp.

The grasping conditions require that a value based on the number of surfaces (i.e. the number of the phalanges) that touch the ball is assigned:

- 2 -> Object contact with at least 3 surfaces
- 0.75 -> Object speed nothing compared to the palm
- 0.5 -> Object speed nothing compared to the phalanges

In figure 10 a graph showing the contact during the time is shown; the graph refers to the contact during the grasping of a sphere having unitary radius. The fluctuating trend in the graph is due to the fact that rebounds may occur due to elastic forces.

4 Conclusion

A model to analyze the grasping of an underactuated finger driven by unextensible tendon was presented. The finger itself is one of those of a mechanical prosthesis that was principally conceived as human prosthesis.

The reported examples seems to indicate that the model can predict the behavior of the finger during the grasping.

The model can be useful for both the under-actuated finger design and for the prediction of the capabilities of the whole hand. Also the actuator’s optimum law of motion, computed by means of a previously proposed algorithm, [19], can represent a field of study that can be improved using the presented model.

Moreover, the model allows measuring the rotations of each phalanx, allowing to test the measurements carried out on real prototypes, by means of previously developed vision systems, [20-23].

The proposed method is also suitable to study several different topics (even very different from this one) the authors are investigating on. Among these, even the dynamics of the throwing machines (see e.g. [25-27]), as for the impact between their component is concerned can be studied.

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References


