

Development of Active Orthosis for Lumbago Relief-Improvement of Pneumatic Textile Actuator for Orthosis -

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Abstract. It is important to develop the orthosis which improves the Quality of Life (QOL) and maintains health conditions. As one of the treatment methods done to lumbago (low back pain), the waist fixation method with the spinal brace or the orthosis is prescribed. A waist active orthosis implemented with pneumatic flexible actuators have been developed. However, several problems of the previous actuator were that the strain and the generated force were small for the orthosis. Thus, this paper propose the improved actuator for the orthosis. The improved actuator is modeled and the reliability of static and dynamic model is validated through experiment. As a result, it was confirmed that the improved actuator had the strain of 2 times and the generated force of 1.3 times, in comparison with the previous actuator. And the dynamic model including volume of actuator could be represented by a second-order form with a dead time.

1 Introduction

It is important to improve the QOL and maintain the health condition for elderly people. Our special attention is directed to lumbago because many people feel a back pain in daily life. As one of the treatment methods done to lumbago, the waist fixation method [1] with a spinal brace or an orthosis is performed. Generally, an orthosis is wrapped around the waist made of cloth and the rubber textile. However, the existing orthosis have the three difficult and important issues.

- 1) Problem difficult to meet on-demand requirements
- 2) Problem to suppress blood stream
- 3) Problem difficult to customize

In order to solve these issues, a waist active orthosis implemented with pneumatic flexible actuators is developed and pressure control method of pneumatic flexible actuators is established. However, the customizing issues have not been solved. In this study, firstly, the prototype of pneumatic textile actuator (hereafter called PTA) has been developed. But several problems of the previous actuator were that the strain and the generated force were small for the orthosis. The previous actuator is indirectly driven by a McKibben actuator. Thus, the improved actuator changes to the driving method that can be contracted directly by a silicone tube. Therefore the improved actuator is modeled and the reliability of static and dynamic model is validated through experiment.

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2 Structure of Improved PTA

The previous PTA has a structure which inwrought with a long McKibben-type actuator[2] into two soft cloths (See Figure 1(a)). When the compressed air is inject into the supply port, the McKibben-type actuator contracts to an axial direction. As the result, the PTA shrinks indirectlyby the seam constraint. Thus, two problems of the previous PTAwere that the strain and the generated force were small for the orthosis.

On the other hand, the improved PTA has a structure which inwrought with a silicone tube into two soft cloths as shown in Figure 1(b).

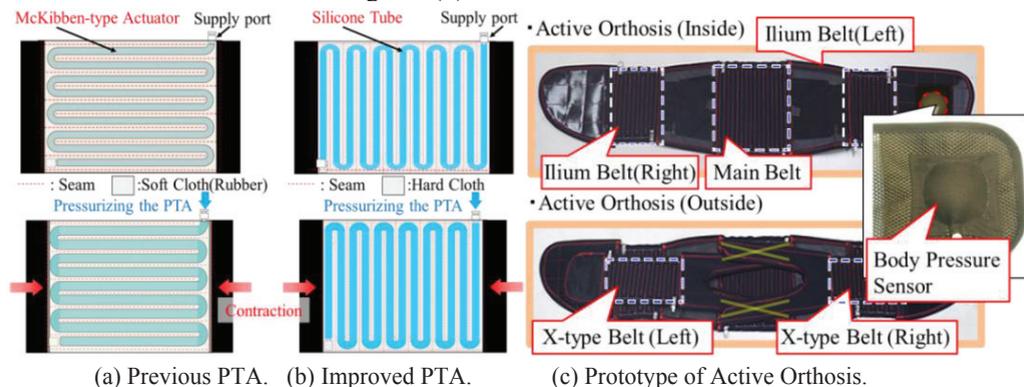


Figure 1. Previous PTA and improved PTA.

Figure 1(c) shows the prototype of the active orthosis for the lumbago relief. The proposed active orthosis consists of five PTAs (=belts) and the body pressure sensor. The size of the orthosis is $970 \times 200 \times 7$ mm, and the mass is 300g. The active orthosis has a double structure. One structure is the body-orthosis that is configured in the main belt and the ilium belts (right and left). Another structure is two X-type belts.

Figure 2(a) shows the operating principle of PTA. When the compressed air is injected into the supply port, the silicone tube expands a radial direction. As the result, the PTA shrinks directly by the constraints of the seam constraint and the hard cloth.

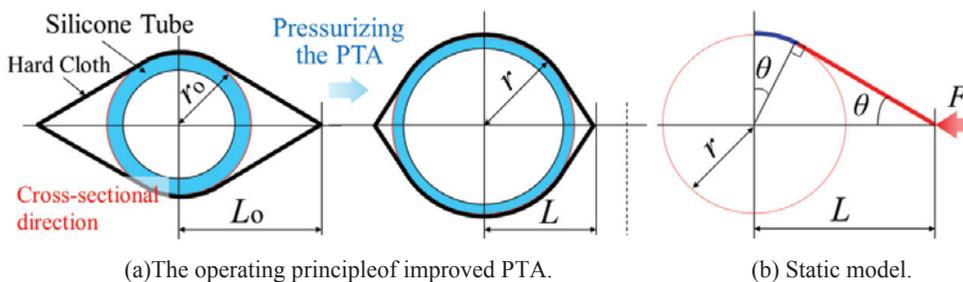


Figure 2. The operating principle and static model of improved PTA.

3 Modeling of Improved PTA

This chapter will be described about the construction methods of a static model and a dynamic model. And the orthoses control valves system is modeled and the reliability of exhaust and supply model is validated through experiment.

3.1 Static Model of Improved PTA

From the view of energy conservation, the input work of the improved PTA should equal the output work which a system includes force dissipation or force loss F_{diss} . Suppose that the actuator is in this ideal condition, a following equation of static model holds.

$$P \cdot dV = -(F + F_{diss}) \cdot dL \tag{1}$$

where P is the internal gauge pressure, dV is the volume change, F is the force generated by the PTA, and dL is the axial displacement, respectively.

When the clothes of PTA are made with the material which can't shrink, the half pitch length b of the seam doesn't change. The outside radius r of the silicone may be expressed as

$$r = b(\theta + \cot \theta)^{-1} \tag{2}$$

where θ is the angle between the seam axis and the silicone (See Figure 2(b)).

The inner volume V of silicone is given by

$$V = l \cdot \pi r_s^2 \tag{3}$$

where r_s is the inside radius and l is length of the silicon, respectively.

Assume that the outside radius r change but the cross-sectional area S_o and the length l of silicone don't change. The following equation is expressed by

$$V = l(\pi r^2 - S_o) \because S_o = \pi(r^2 - r_s^2) = Const. \tag{4}$$

Eq.(2) is substituted for eq.(4). Then, the inner volume V can be rewritten as

$$V = l \{ \pi b^2 (\theta + \cot \theta)^{-2} - S_o \} \tag{5}$$

On the other hand, since the force term $F + F_{diss}$ of eq.(1) is given by

$$F + F_{diss} = -P \frac{dV}{dL} = -P \frac{\partial V}{\partial \theta} \cdot \frac{\partial \theta}{\partial L} \tag{6}$$

Hence, the generated force F is

$$F = 2\pi lbP \left\{ \frac{\cos \theta}{\theta(\theta + \cot \theta)} \right\} - F_{diss} \tag{7}$$

where each partial differentiation with eq.(6) is

$$\frac{\partial V}{\partial \theta} = \frac{2\pi lb^2 \cot^2 \theta}{(\theta + \cot \theta)^3}, \quad \frac{\partial L}{\partial \theta} = -\frac{b\theta \cos \theta}{(\theta \sin \theta + \cos \theta)^2} \tag{8}$$

The length L is the involute function with respect to θ . Thus, the angle θ is the nonlinear inverse-function with respect to L . However, the inverse function of an involute function can't be solved analytically. In this paper, this inverse function will be solved numerically.

Therefore, to solute the nonlinear function $f(\varepsilon)$ that is the first term of right side in eq.(7), the relation between the function $f(\varepsilon)$ and the strain ε is calculated by the numerical solution such as Newton method.

$$f(\varepsilon) = \frac{\cos \theta}{\theta(\theta + \cot \theta)} \because \varepsilon = \frac{L - L_o}{L_o} \tag{9}$$

where L_o denotes an initial length of PTA.

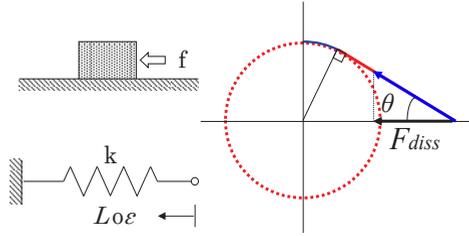


Figure 3.Concept of dissipation force F_{diss} .

If a strain of the PTA is held in less than 25 percent, the function $f(\varepsilon)$ with respect to strain ε is approximated by following first-order function.

$$f(\varepsilon) = \frac{\cos \theta}{\theta(\theta + \cot \theta)} \equiv \alpha \cdot \varepsilon + \beta \tag{10}$$

where α and β are characteristics parameters of PTA.

Eq.(10) is substituted for eq.(7). The generated force F is given by

$$F = 2\pi lbP(\alpha \cdot \varepsilon + \beta) - F_{diss} \tag{11}$$

Then, the dissipation force is discussed. In this paper, the dissipation force F_{diss} includes a static frictional force and the force loss of an elastic force which occur to the silicone and the cloth. Figure 3 shows the concept of dissipation force F_{diss} .

The static model of the improved PTA with the dissipation force is expressed by

$$F = 2\pi lbP(\alpha \cdot \varepsilon + \beta) - (kL_0\varepsilon + f) \cos \theta \tag{12}$$

where k is an elastic coefficient and f is a static frictional force.

Furthermore, we discuss the relation between strain ε and cosine function that is the second term of right side in eq.(12). If a strain of the PTA is held in less than 20 percent, the function $\cos(\theta)$ with respect to strain ε is approximated by following first-order function.

$$\cos \theta \equiv \gamma \cdot \varepsilon + \eta \tag{13}$$

where γ and η are the approximate coefficients of the cosine function.

Eq.(13) is substituted for eq.(12). Therefore, the static model of the improved PTA is given by

$$F = P(\alpha_1\varepsilon + \alpha_0) - (\beta_2\varepsilon^2 + \beta_1\varepsilon + \beta_0) \tag{14}$$

where coefficients $\alpha_1 = 2\pi lb\alpha$, $\alpha_0 = 2\pi lb\beta$, $\beta_2 = kL_0\gamma$, $\beta_1 = kL_0\eta + f\gamma$ and $\beta_0 = f\eta$ are PTA characteristics constants, respectively. Clearly, the force F depends on both pressure P and strain ε . When pressure increases, the silicone tube expands radially and PTA shortens in length to generate a radial contraction force.

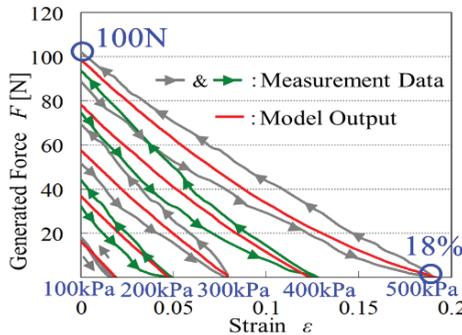


Figure 4.Verification experiment of static model (Results of measurement and model output signals).

In order to prove versatility of equation (14), the comparison was done between the measurement data and force model. It can be seen in Figure 4 that both generated force F and strain ϵ increase with pressure. The static force model of the improved PTA is that it is located in the average of the hysteresis loop. Therefore, the accurate fitting is demonstrated in Figure 4. And, The improved actuator had the strain performance of 2 times and the generated force of 1.3 times, in comparison with the previous actuator.

3.2 Three Modes of Tested Valve

Figure 5 shows the operating principle of the orthosis control valve. The tested valve consists of two on/off-type control valves (SMC Co. Ltd., S070C- SDC-32) that both output ports are connected each other. One valve is used as the supply valve, and another is used as the exhaust valve. Two valves can adjust output flow rate like a variable fluid resistance by means of the fast switching. The size of the on/off valve is $36 \times 14.5 \times 7.2$ mm, and the mass is 5 g. The total mass of the orthosis control valve including the controller (Micro-computer: Renesas Co. Ltd., H8/3664F) is very light, that is about 220 g. The orthosis control valve has three modes (See Figure 5(a), (b) and (c)) as follows:

- (a) Supply Mode: The exhaust valve is the off state. And, the pressure of the tank (PTA) can be adjusted by the fast switching of the supply valve.
- (b) Exhaust Mode: Conversely, the supply valve is the off state. And, the pressure of the tank (PTA) can be adjusted by the fast switching of the exhaust valve.
- (c) Hold Mode: When both valves are the off states, the pressure of the tank (PTA) is kept a constant pressure.

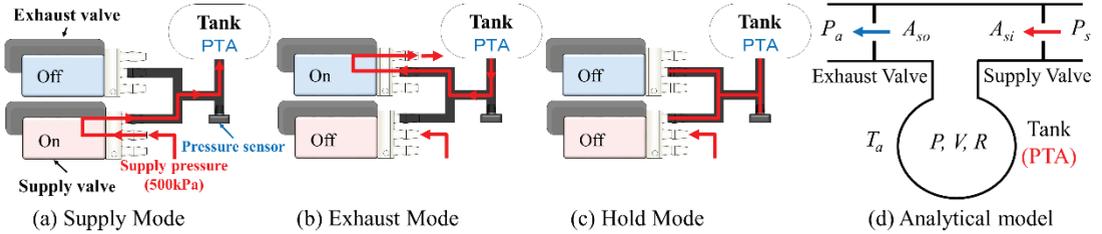


Figure 5. Three Modes and analytical model of the orthosis control valve.

3.3 Dynamic Model of Improved PTA[3] [4]

Figure 5(d) shows the analytical model of the orthosis control valve. The mass flow rate of supply valve Q_i and the exhaust valve Q_o are given as follows.

$$Q_i = A_{si} P_s \sqrt{\frac{2}{RT_a}} g(z_i), \quad z_i = \frac{P}{P_s} \quad \text{Supply State} \quad (15)$$

$$Q_o = A_{so} P_a \sqrt{\frac{2}{RT_a}} g(z_o), \quad z_o = \frac{P}{P_a} \quad \text{Exhaust State} \quad (16)$$

where R and T_a mean a gas constant and an absolute temperature, respectively. The function $g(z)$ that expresses the state of flow is given as follows.

$$g(z) = \sqrt{\frac{\kappa}{\kappa-1} \left(z^{2/\kappa} - z^{(\kappa+1)/\kappa} \right)} \quad [0.528 \leq z \leq 1] \text{ Subsonic Flow} \quad (17)$$

$$g(z) = \sqrt{\frac{\kappa}{\kappa+1} \left(\frac{2}{\kappa+1} \right)^{2/(\kappa-1)}} \quad [0 \leq z \leq 0.528] \text{ Choked Flow} \quad (18)$$

where κ means a specific heat ratio (=1.4). The pressure P in the volume V of PTA is given by next equation.

$$\dot{P} = \frac{dP}{dt} = \frac{\kappa RT_a}{V} (Q_i) \quad : \text{Supply State} \quad (19)$$

$$\dot{P} = \frac{dP}{dt} = \frac{\kappa RT_a}{V} (-Q_o) \quad : \text{Exhaust State} \quad (20)$$

The system of Eqs.(19) and (20) are non-linear systems with respect to the input of sectional area A_{s*} (*=i or o). Here, the simple idea is to approximate a non-linear system by a linear one (around the pressure point $P=P_E$ ($z=0.528$))

$$\dot{x} = -\frac{2.70 \times 10^2 \cdot A_{so}}{V} x - \frac{4.61 \times 10^4}{V} v \quad \because x = P_E - P, v = A_o \quad : \text{Supply State} \quad (21)$$

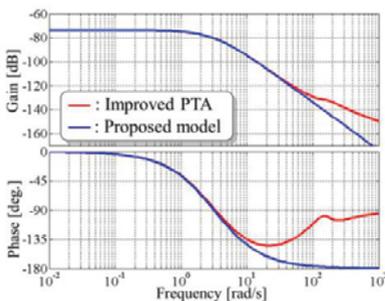
$$\dot{x} = -\frac{2.78 \times 10^2 \cdot A_{si}}{V} x + \frac{4.68 \times 10^4}{V} v \quad \because x = P_E - P, v = A_i \quad : \text{Exhaust State} \quad (22)$$

In the linearization, the atmospheric pressure P_a of 101.3 kPa, the room temperature T_a of 298 K, the gas constant R of 287 J/kg/K, the supply pressure P_s of 500 kPa were used. And the sectional area of the supply port A_{si} ($=2.02 \times 10^{-7} \text{ m}^2$) and the area of exhaust port A_{so} ($=2.30 \times 10^{-7} \text{ m}^2$) were adopted the values of catalog specification (on/off valve). The obtained linear system can be expressed by the first-order transfer function. The pole of first-order system depends on the volume V of PTA. The smaller volume of PTA, the faster response speed becomes.

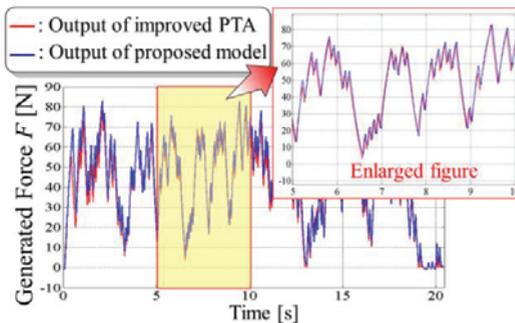
On the other hand, suppose that the sectional area $v=A_*$ of the on/off valve is opened (or closed) slowly. Suppose that the switching area A_* (*=i or o) of valve is approximated by dead time L (=3 ms) and time constant T_o (=2 ms) of a primary delay system.

$$v(s) = A_*(s) = \frac{A_{s*}}{T_o s + 1} \cdot e^{-Ls} \cdot u(s) \quad \left\{ \begin{array}{l} u(s) = 1 \quad : \text{Supply Mode} \\ u(s) = -1 \quad : \text{Exhaust Mode} \\ u(s) = 0 \quad : \text{Hold Mode} \end{array} \right. \text{New Input} \quad (23)$$

From Eqs.(21)-(23), the transfer function of on/off valve system with volume of PTA is given by a second-order form and a dead time. The transfer function of the control valve system with volume of PTA is given by a second-order form with a dead time [5]. To validate the reliability of the linear model, the verification experiment of supply (500 kPaG) and exhaust (0 kPaG) motion was performed on conditions of different volumes. Figure 6(a) shows the result (bode diagram) of system identification using the experimental device. And, Figure 6(b) shows the experimental result and output of the proposed model at the volume $V=7 \text{ ml}$. From Figure 6(b), it can be seen that the output results (rise action and fall action) using the proposed model agree well with the experimental result. The proposed model was a very simple model, but it could be confirmed that the actual valve system including volume can be represented by means of a second-order form with a dead time.



(a) Bode diagram of valve system.



(b) Experimental results of dynamic model

Figure 6. Results of verification experiment.

4 Conclusions

This study was aimed to develop the PTA of the orthosis for lumbago relief and the resulting knowledges are summarized as follows:

- 1) The improved PTA was modeled and the reliability of static and dynamic model was validated through experiment.
- 2) The improved actuator had the strain performance of 2 times and the generated force of 1.3 times, in comparison with the previous actuator.
- 3) The dynamic model including volume of PTA could be represented by means of a second-order form with a dead time.

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