Large magnetocaloric effects in magnetic intermetallics: First-principles and Monte Carlo studies

Peter Entel1, a, Markus E. Gruner1, 2, Masako Ogura3, Vladimir V. Sokolovskiy4, Vasily D. Buchelnikov4, Anna Grünebohm1, Raymundo Arróyave5, Kazuhiro Uebayashi6, Navdeep Singh7, Anjana Talapatra5, Thien Duong5, Mehmet Acet1 and Aslı Çakır1, 8
1University of Duisburg-Essen, Faculty of Physics and CENIDE, 47048 Duisburg, Germany
2Forschungs-Neutronenquelle Heinz-Maier-Leibnitz (FRM II), TU München, 85748 Garching, Germany
3Department of Physics, Osaka University, Machikaneyama 1-1, Osaka 560-0043, Japan
4Condensed Matter Physics Department, Chelyabinsk State University, 454021 Chelyabinsk, Russia
5Department of Materials Science and Engineering, University of Texas A&M, College Station, Texas 77843, USA
6NIT, Akita College, Akita, Japan
7Department of Engineering and Technology, University of Houston, Houston, Texas 77204, USA
8Metallurgical and Materials Engineering Department, Mugla University, Mugla, Turkey

Abstract. We have performed ab initio electronic structure calculations and Monte Carlo simulations of frustrated ferroic materials where complex magnetic configurations and chemical disorder lead to rich phase diagrams. With lowering of temperature, we find a ferromagnetic phase which transforms to an antiferromagnetic phase at the magnetostructural (martensitic) phase transition and to a cluster spin glass at still lower temperatures. The Heusler alloys Ni-(Co)-Mn-(Cr)-(Ga, Al, In, Sn, Sb) are of particular interest because of their large inverse magnetocaloric effect associated with the magnetostructural transition and the influence of Co/Cr doping. Besides spin glass features, strain glass behavior has been observed in Ni-Co-Mn-In. The numerical simulations allow a complete characterization of the frustrated ferroic materials including the Fe-Rh-Pd alloys.

1 Introduction

The widely used intermetallics Ti-Ni have attracted much interest over decades because of their martensitic transformation, superelasticity and excellent shape memory behavior [1] and new glass phases [2]. With magnetism as additional degree of freedom, magnetic shape memory Heusler alloys have been found with large reversible deformations under the application or removal of a magnetic field [3]. The strong coupling between magnetism and structure leads to a first order magnetostructural transition with different magnetization of austenite and martensite because of different magnetocrystalline anisotropy and different magnetic exchange coupling constants. The stronger anisotropy of the martensitic phase allows rotation of the martensitic variants under the application of a magnetic field, leading to the magnetic shape memory effect [4]. Magnetic superelasticity is involved in the stabilization of the phase with highest magnetization in an external magnetic field [5, 6]. In addition to shape memory and superelasticity, these alloys (ternary magnetic shape memory Heusler alloys of type Ni-(Co)-Mn-(Cr)-(Al, Ga, In, Sn, Sb)) exhibit magnetocaloric (conventional and inverse) [7, 8, 9], barocaloric [10] and elastocaloric [11] effects, magneto-resistance [12], exchange bias [13] and kinetic arrest [14]. Also spin-glass [15] and strain-glass [16] features have been reported on several of these Heusler alloys.

In this short communication, we compare the structural and magnetic behavior and magnetocaloric properties of cubic Heusler alloys shown in Fig. 1 with some of the giant magnetocaloric materials known before like Gd5(Si2Ge)2 (monoclinic crystal structure) [17], La(Fe13-xSix) (cubic NaZn13 D23-type structure) [18], and Fe-Rh (cubic CsCl-type structure) [19]. The comparison shows remarkable similarities associated with the inverse magnetocaloric effect emerging from the magnetostructural transition in the magnetic Heusler alloys with the corresponding magnetostructural transition and calorific effect of the Gd based and Fe-Rh-Pd based compounds as discussed below.

2 Structural and magnetic phase diagrams of Heusler intermetallics

Figure 1 shows the intersection of structural and magnetic phase transitions in the phase diagrams of Ni-Mn-Ga and Ni-Mn-In as a function of the valence electron concentration [20, 21]. The ab initio calculations in combination with Monte Carlo simulations reproduce fairly well the experimental phase diagrams, which have been discussed in [3].
Figure 1. Phase diagrams of Ni-Mn-Ga and Ni-Mn-In in the temperature versus electron concentration plane in comparison with experimental data (open circles mark the martensitic transformation temperature $M_S$ taken from various sources, see [3]. Dark lines (blue, indigo) mark martensitic L2$_1$-L1$_0$ transformation temperatures (from ab initio total energy differences between austenite and martensite [20, 21]) and Curie temperatures (from Monte Carlo simulations using ab initio magnetic exchange coupling constants [20, 21]), respectively. Recent ab initio calculations have been done along the path marked by the arrow in each phase diagram.

Special attention is given in this paper to the magnetic properties of the non-stoichiometric Ni-Mn-Ga and Ni-Mn-In Heusler alloys (see [22] for the case of Ni$_{50}$Mn$_{34}$In$_{16}$).

Figure 2 shows that the materials do not form homogeneous alloys, instead we observe a multiplicity of coexisting non-modulated (L1$_0$) and modulated (5M, 7M) intermediate martensitic structures because of chemical clustering effects in the alloys [23, 24]. This also leads to multiple spin configurations. Especially in the case of Mn-excess in X$_2$Y$_{1+x}$Z$_{1-x}$ alloys, where the excess Mn$_Y$ atoms mostly go onto the Z sites, which is accompanied by a spin flip transition because of the antiferromagnetic exchange coupling constant between Mn$_Y$ on its original sublattice and Mn$_Z$ on the Z sublattice. This is because the distance between nearest neighbor Mn atoms on the Mn sublattice is $a\sqrt{2}/2$, where $a$ is the lattice constant of the cubic L2$_1$ structure, causing ferromagnetic order, which is reduced to $a/2$ for nearest neighbor Mn$_Y$ and Mn$_Z$ atoms, causing antiferromagnetic order. Since the magnetic moment of Mn is $\approx 4\, \mu_B$, this spin flip has a large effect and leads to metamagnetic behavior of the Mn-based Heusler alloys (see also [21, 25]). This is discussed in more detail below.

3 Energy variation of magnetic Heusler alloys along the Bain path

Figure 3 shows the Energy variation, E(c/a), at zero temperature of Ni$_{50}$Mn$_{31.25}$Ga$_{21.75}$ (using a Ni$_{8}$Mn$_{5}$Ga$_{3}$ supercell to approximate the alloy) and the effect of Co-doping using a Ni$_7$Co$_1$Mn$_5$Ga$_3$ supercell [24] along the Bain path showing the stability of the L1$_0$ martensitic phase at low temperature.

With increasing temperature (which can be simulated using the fixed spin moment method allowing to calculate binding curves at reduced magnetization) “ferro” and “ferri” solutions move relative to each other until the “ferro” solution becomes lower in energy at the martensitic to austenitic transition.

The magnetic exchange coupling constants can be obtained from ab initio calculations [24] and are plotted in Fig. 4 for the case of Mn-excess Ni$_{50}$Mn$_{19}$Ga$_{30}$ compared to stoichiometric Ni$_5$MnGa. The chemical disorder caused by Mn excess introduces negative magnetic coupling constants (antiferromagnetic exchange interactions) which weaken the ferromagnetic spin configuration and lead to magnetic clustering effects which have been detected by neutron scattering experiments [25]. Ni$_{50.1}$Co$_{10}$Mn$_{19}$Sn$_{10}$ reveals an unusually large change (jump) of $M(T)$ at the martensitic transition.
Ferromagnetism in the austenitic phase and “ferri” (spins on the Mn2 sublattice are reversed), antiferromagnetism or parmagagnetism in the martensitic phase [26, 27]. There are ferromagnetic spin clusters of nanoscopic dimensions with center-to-center spacing around 12 nm [25]. This is the origin of metamagnetic behavior: a magnetic field applied to martensite can yield a first order transition to the ferromagnetic austenitic phase (see, for example, [28]). When adding Co to the Heusler alloys for getting better magnetocaloric effects, the magnetostructural transition is shifted to lower temperatures because of decrease of e/a and eventually the martensitic phase vanishes altogether for larger Co concentration.

The resulting adiabatic temperature change $\Delta T_{ad}$ for this alloy is still quite small (1.6 K) in spite of the large change of $M$ showing that the magnetocaloric effect (MCE) needs further optimization compared to the classical Gd-Si-Ge, Fe-Rh and La-Fe-Si MCE materials, which all display $\Delta T_{ad}$ of about 13 K and a large isothermal entropy change $\Delta S_{iso}$. There have been many attempts to improve the MCE in Heusler and other intermetallics which has been highlighted in the literature [31]. A discussion of the magnetostructural transition and adiabatic temperature variation in poly-crystal and single crystal Ni-Mn-Ga alloys can be found in [32].

It is very interesting to note that the binary system Fe-Rh also displays a large jump of the magnetization which can be considered as a relict of the magnetostructural transition of the ternary Rh(Fe$_{1-x}$Pd$_x$) alloy system for vanishing Pd concentration [33]. See also discussion of FePd, MnRh and MnPd compounds in comparison to FeRh [34]. The recent publications regarding the magnetization dynamics across the first order phase transition in FeRh thin films [35] and the temperature induced metamagnetic transition and domain structures of single-crystalline FeRh thin films on MgO(100) [36] show the ongoing interest in this classical magnetocaloric material [37]. Magnetostuctural transition has also been discussed for B2-ordered FeRh epiayers which show coexistence of lattice expanded and contracted phases in spatially different regions [38] as well as coexistence of FM and AFM in the epiayers [39].

Figure 6 shows the existence of a magnetostructural transition in the Fe-Rh-Pd alloys. Regarding the magnetization behavior of FeRh in Fig. 7, we find a striking similarity to the variation of $M(T)$ over the magnetostructural transition in Heusler alloys (as in Fig. 5). We are currently performing calculations of the magnetocaloric effect in FeRh and its alloys.
Figure 6. Calculated total energies of Fe(Rh$_{1-x}$Pd$_x$) for (a) $x = 0$ and (b) $x = 0.2$ for FM and AFM alignment (AF3 type stacking of (100) AFM layers in [001] direction, neighboring Fe layers couple AFM like) as a function of $c/a^*$, where $a^*$ is the lattice constant of CuAu-I type ordered structure which gives the CsCl structure for $c/a^* = 1$. (b) shows the structural transition for the AFM solution with the minimum of energy moving from $c/a^* = 1$ to $c/a^* > 1$. The virtual crystal approximation (VCA) has been used in the calculations with $a^* = 3$ Å which is very close to the observed one, $a^* = 2.99$ Å (data from [33]). For larger $x$ ($x = 0.525$) the FM phase with orthorhombic structure becomes the ground state for Fe(Rh$_{1-x}$Pd$_x$) [37].

Figure 7. $M(T)$ curves of Fe-Rh on cooling and heating in zero magnetic field [19]. The magnetic collapse at the FM-AFM transition shows similarities with the corresponding large change of magnetization at the magnetostructural transition. Compare also the results of neutron scattering experiments [40]. The FM alignment is within the (111) planes and the AFM alignment is between (111) planes. 

Ab initio calculations essentially confirm this. The AFM type of order yielding the lowest energy state, is of AF3 type [33].

Note that similar magnetization curves as in Fig. 7 have also been obtained for the anti-perovskite Mn$_3$GaC [41].

The large change of the magnetization, which is associated with the metamagnetic phase gives rise to a large inverse magnetocaloric effect compared with the conventional MCE at the Curie temperature.

5 The atomistic origin of metamagnetic transitions in magnetic intermetallics

In the same way as we find magnetism dominated by competing FM-AFM interactions in the non-stoichiometric Heusler Ni$_{30}$Mn$_{30}$Ga$_{20}$ alloys as shown in Fig. 4(b), we observe coexistence of such interactions in FeRh materials, too. Figure 8 shows corresponding results for the element-resolved magnetic coupling constants of FeRh. The corresponding orbital resolved $J_{ij}$ have also been calculated recently.

In conclusion, there is similarity between Fe-Rh and Ni-Mn-(Ga, In) alloys regarding the coexistence of FM and AFM interactions. These arise from the competing exchange interactions involving the $e_g$ and $t_{2g}$ orbitals. With respect to the AFM-FM transition at the magnetostructural transition in Ni-Mn-In, we may interpret this (in much the same way as in Invar alloys) as a low-spin-to-high-spin (LS-HS) transition. Indeed, the LS-HS scenario shows up when we calculate the energy (with energetically nearly degenerate LS and HS states) or the individual magnetic moments of the atoms as a function of fixed magnetization per unit cell. This so called fixed spin moment method has been successfully used to describe magnetic anomalies in magnetic transition metal compounds. Figure 9 shows, e.g., the existence of a low-spin-high-spin (LS-HS) transition in Ni$_{50}$Mn$_{37.5}$In$_{12.5}$ (using a cubic 16-atom supercell of Ni$_8$Mn$_6$In$_2$).

A similar LS-HS scenario as in Fig. 9 is achieved for other disordered magnetic Heusler alloys, too. Also, if in addition to the fixed spin moment condition, we constrain other moments to undergo a spin-flip transition, we observe many energetically close lying LS states as shown in Fig. 10 for the case of Ni$_7$Co$_1$Mn$_7$Sn$_1$.

In the following we show results for the magnetocaloric effect calculated with the help of ab initio calculations and Monte Carlo simulations [22, 29] in comparison to experimental data. In the Monte Carlo study we use an effective spin model which includes elastic and magnetoelastic interactions. We limit the discussion to the case of Co-doped Ni-(Co)-Mn-In, for which it is known that Co enhances considerably the MCE. Regarding the spin-spin interactions, we have used a Potts model, which allows to keep track of the various spin multiplicities such as $S = 5/2$ for Mn$^{3+}$, $S = 1$ for Ni$^{2+}$, $S = 3/2$ for Co$^{2+}$ and $S = 4/2$ for Cr$^{2+}$. For details, see [22, 24, 29].
Figure 9. Variation of magnetic moments of the 6 Mn atoms in the 16-atom supercell of austenitic Ni₈Mn₆In₂ as a function of the fixed magnetization of the cell. The two Mn on the In sublattice, labeled Mn3 and Mn6, have their spins flipped leading to the low-spin state (LS), which is nearly energetically degenerate with the high-spin state (HS), see Fig. 10.

Figure 10. Energy variation of LS and HS states for the 16-atom unit cell of austenitic Ni₇Co₃Mn₇Sn₁ as a function of the fixed magnetization of the cell. The three Mn on the Sn sublattice have their spins flipped leading to the low-spin state (LS; “ferri”), which is nearly energetically degenerate with the high-spin state (HS; “ferro”). Shown are other LS states achieved by different spin reversals, for example, 1 Mn ex, 2 Mn, which means 1 Mn on the Sn sublattice and 2 Mn on their regular sublattice have their spins reversed. Note, however, that this has been obtained without relaxation of atomic positions.

6 Magnetocaloric effect of metamagnetic Ni₄₅Co₅Mn₃₇In₁₃ alloys

The structural and magnetic properties (including magnetic exchange coupling constants) have been calculated using ab initio method whereas the thermodynamic properties and MCE have been obtained from Monte Carlo simulation, using

\[ \Delta T_{ad}(T, H) \approx -\frac{\Delta S_{mag}(T, H)}{C(T, H)} \]  

(1)

whereby the entropy change across the magnetostructural transition in an external magnetic field is obtained by integrating the specific heat (using a model Hamiltonian which consists of magnetic, elastic and magnetoelastic terms, see [42]). In Eq. (1), the specific heat is the total specific heat (magnetic, electronic plus lattice part).

Figure 11 shows the final result for the conventional and inverse entropy and adiabatic temperature changes for Ni₄₅Co₅Mn₃₇In₁₃. The result compares well with the experimental data of Liu et al. [43]. In summary, we may say that the large jump of the magnetization at the first order magnetostructural transformation leads to the large entropy and adiabatic temperature changes. Cobalt enhances the magnetization of the austenitic phase favoring the large change of magnetization at the martensitic transformation and simultaneously leads to the undercooling effect of the austenitic phase.

Figure 11. Adiabatic temperature change of the direct (filled circles) and inverse (filled squares) magnetocaloric effect of polycrystalline Ni₄₅Co₅Mn₃₇In₁₃ as obtained from the extended spin model. Diamonds mark results for a single domain phase while the inset shows the variation of the entropy [29].

The magnetic cooling effect shown here does not yet reach the values of the Gd, La or Fe-Rh compounds but values tend already to reach 10 K. If, in addition, the problem of magnetic and thermal hysteresis can be solved, these Heusler alloys appear to be attractive materials for future refrigeration technologies.

7 Conclusion

The combined effort of using ab initio tools in combination with Monte Carlo methods allows to establish phase diagrams as well as functional materials properties at finite temperatures such as the magnetocaloric effect of intermetallics. The results show agreement with experiment and also allow predictions of how to improve the functionalities of these 'intelligent' materials.

The authors P.E., A.G. M.A. and A.Ç. acknowledge support by the DFG through the Priority Programme 1599 on “Ferroic Cooling”, and M.E.G. by SFB TRR80.
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