

## Adaptive nonlinear control of single-phase to three-phase UPS system

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**Abstract.** This work deals with the problems of uninterruptible power supplies (UPS) based on the single-phase to three-phase converters built in two stages: an input bridge rectifier and an output three phase inverter. The two blocks are joined by a continuous intermediate bus. The objective of control is threefold: i) power factor correction "PFC", ii) generating a symmetrical three-phase system at the output even if the load is unknown, iii) regulating the DC bus voltage. The synthesis of controllers has been reached by two nonlinear techniques that are the sliding mode and adaptive backstepping control. The performances of regulators have been validated by numerical simulation in MATLAB / SIMULINK.

### 1 Introduction

Uninterruptible power supplies (UPS) play an important role in interfacing critical loads such as computers, communication systems, medical/life support systems, and industrial controls to the utility power grid. They are designed to provide clean and continuous power to the load under essentially any normal or abnormal utility power condition.

In this work, we focus on adaptive nonlinear control for single phase to three-phase UPS system figure1, which is based on the single-phase bridge rectifier, three-phase inverter and an LC filter. All IGBT- diode switches with PWM control, to ensure control the DC component of the output of the rectifier, the correction of the power factor and generating a symmetric three phase system. To achieve these objectives three control loops are used in [1], [2].

The first inner loop is designed, using the sliding mode technique, to ensure PFC. The second inner loop is designed, using the adaptive backstepping approach, to generating a symmetrical three-phase system with a three-phase resistive load supposed unknown. The outer-loop involves a PI regulator that regulates the DC bus voltage [3].

This paper is organized as follows: Section 2 is devoted to the description and modelling of single-phase to three-phase UPS System, the synthesis of regulators is developed in section 3. The closed loop performances are illustrated by simulation in Section 4. The conclusion ends the paper.

### 2 System Descriptions and Modelling

The single-phase to three-phase UPS system under study has the structure of Figure 1. At the same time, the two legs, IGBT-diode, works as a bridge rectifier and supply the DC-link bus with power. The other three legs work in inverter mode and feed the loads.

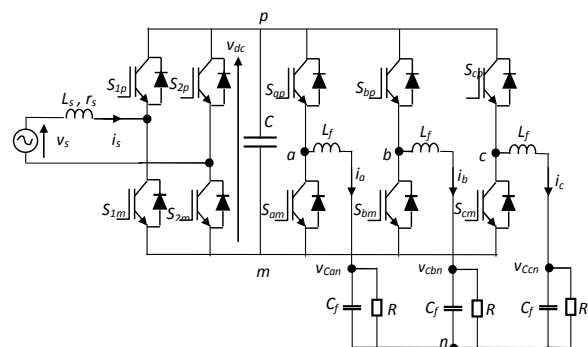


Fig .1. Single-phase to three-phase UPS system.

The switching functions  $\mu$  and  $\mu_j$  are defined by :

$$\mu = \begin{cases} 1 & \text{if } S_{1p}, S_{2m} \text{ are ON and } S_{2p}, S_{1m} \text{ are OFF} \\ -1 & \text{if } S_{2p}, S_{1m} \text{ are ON and } S_{1p}, S_{2m} \text{ are OFF} \end{cases}$$

$$\mu_j = \begin{cases} 1 & \text{if } S_{jp} \text{ is ON and } S_{jm} \text{ is OFF} \\ -1 & \text{if } S_{jm} \text{ is ON and } S_{jp} \text{ is OFF} \end{cases} \quad (j = a, b, c)$$

The average model, in dq frame, thus obtained is described by three subsystems as follow:

$$L_s \frac{dx_s}{dt} = -r_s x_s + v_s - u x_{dc} \quad (1)$$

$$\frac{d}{dt} \begin{pmatrix} x_{1d} \\ x_{1q} \end{pmatrix} = \begin{pmatrix} 0 & \omega \\ -\omega & 0 \end{pmatrix} \begin{pmatrix} x_{1d} \\ x_{1q} \end{pmatrix} + \frac{1}{C_f} \begin{pmatrix} x_{2d} \\ x_{2q} \end{pmatrix} - \delta \begin{pmatrix} x_{1d} \\ x_{1q} \end{pmatrix} \quad (2a)$$

$$\frac{d}{dt} \begin{pmatrix} x_{2d} \\ x_{2q} \end{pmatrix} = \begin{pmatrix} 0 & \omega \\ -\omega & 0 \end{pmatrix} \begin{pmatrix} x_{2d} \\ x_{2q} \end{pmatrix} + \frac{x_{dc}}{2L_f} \begin{pmatrix} u_d \\ u_q \end{pmatrix} - \frac{1}{L_f} \begin{pmatrix} x_{1d} \\ x_{1q} \end{pmatrix} \quad (2b)$$

$$C \frac{dx_{dc}}{dt} = u x_s - \frac{1}{2} (u_d x_{2d} + u_q x_{2q}) \quad (3)$$

where the various state variables are the average values, over cutting periods, of the physical variables, see table 1:

**Table 1.** The average values, over cutting periods, of the physical variables

State variable	Is the average values of
$x_s$	$i_s$
$x_{dc}$	$v_{dc}$
$x_{1d}, x_{2d}$	$v_{Cd}, i_d$
$x_{1q}, x_{2q}$	$v_{Cq}, i_q$

Notice that the model of three subsystems (1), (2a-b) and (3) is clearly nonlinear and the mean values  $u$ ,  $u_d$  and  $u_q$  of  $\mu$ ,  $\mu_d$  and  $\mu_q$  turn out to be the system control inputs. The parameter  $\delta = 1/RC_f$  is unknown, because the load resistance  $R$  is assumed unknown.

### 3 Controller Design

The aim is to design a controller which is able to achieve three follows objectives:

PFC requirement: the current drawn by the single phase rectifier should be, in average, in phase with the grid voltage.

Output voltage regulation: the three-phase inverter must generate a symmetrical three-phase system despite the fact that the load resistance is unknown.

DC link voltage regulation: the DC component of the voltage must be stabilized to a desired reference voltage.

#### 3.1 PFC inner loop design

Based on the first sub-system (1), The PFC objective is achieved by the regulator, using the sliding mode control [4], [5], that enforces the current  $x_s$  to track a reference signal of the form  $x_s^* = \beta v_s(t)$ , while  $\beta$  is a positive real signal to be defined later.

Consider the sliding surface  $S(x_s)$  defined by:

$$S(x_s) = e_i = x_s - x_s^* \quad (4)$$

The convergence condition is defined by the Lyapunov function  $V = 0.5S^2(x_s)$  as follows:

$$\dot{V} = S(x_s) \dot{S}(x_s) < 0 \quad (5)$$

The equivalent component can be interpreted as the average value modulated, we obtain:

$$u_{eq} = \frac{1}{x_{dc}} (-r_s x_s + v_s) \quad (6)$$

The non-linear component is determined to ensure the attraction of current to the sliding surface and satisfy the convergence condition described by (5), then:

$$u_n = c_i \frac{L_s}{x_{dc}} \text{sgn}[S(x_s)] \quad (7)$$

The sliding mode control law is as follows:

$$u = \frac{1}{x_{dc}} \left\{ -r_s x_s + v_s + c_i L_s \text{sgn}[S(x_s)] \right\} \quad (8)$$

#### 3.2 Three-phase system inner loop design

The controller must force the three-phase system voltage of three-phase inverter DC / AC to track reference signals with the reference signals in dq frame follow:

$$\begin{pmatrix} x_{1d}^* & x_{1q}^* \end{pmatrix} = \begin{pmatrix} 0 & -\sqrt{3/2} E \end{pmatrix} \quad (9)$$

The synthesis technique used is known as the adaptive backstepping and is completed in two steps.

**Step 1:** Stabilization of the subsystem  $(e_{1d}, e_{1q}, \delta)$

Consider the tracking error vector  $E_I$  defined by :

$$E_I = \begin{pmatrix} e_{1d} \\ e_{1q} \end{pmatrix} = \begin{pmatrix} x_{1d} - x_{1d}^* \\ x_{1q} - x_{1q}^* \end{pmatrix} \quad (10)$$

and its dynamics is given by:

$$\dot{E}_I = \begin{pmatrix} \dot{e}_{1d} \\ \dot{e}_{1q} \end{pmatrix} = \begin{pmatrix} \omega x_{1q} + x_{2d}/C_f - \delta x_{1d} - \dot{x}_{1d}^* \\ -\omega x_{1d} + x_{2q}/C_f - \delta x_{1q} - \dot{x}_{1q}^* \end{pmatrix} \quad (11)$$

We use the following Lyapunov candidate function:

$$W_I = \frac{1}{2} e_{1d}^2 + \frac{1}{2} e_{1q}^2 + \frac{1}{2\gamma} \delta^2 \quad (12)$$

Its derivative with respect to time is given by:

$$\begin{aligned} \dot{W}_I = e_{1d} & \left( \omega x_{1q} + \frac{1}{C_f} x_{2d} - \hat{\delta} x_{1d} - \dot{x}_{1d}^* \right) \\ & + e_{1q} \left( -\omega x_{1d} + \frac{1}{C_f} x_{2q} - \hat{\delta} x_{1q} - \dot{x}_{1q}^* \right) - \frac{1}{\gamma} \dot{\delta} \left( \hat{\delta} + \gamma (x_{1d} e_{1d} + x_{1q} e_{1q}) \right) \end{aligned} \quad (13)$$

If  $x_{2d}/C_f = \sigma_d$  and  $x_{2q}/C_f = \sigma_q$  was our effective control,  $\sigma_d$  and  $\sigma_q$  are suitable stabilizing functions, it is sufficient to take:

$$\begin{cases} \sigma_d = -c_{1d} e_{1d} - \omega x_{1q} + \hat{\delta} x_{1d} + \dot{x}_{1d}^* \\ \sigma_q = -c_{1q} e_{1q} + \omega x_{1d} + \hat{\delta} x_{1q} + \dot{x}_{1q}^* \end{cases} \quad (14)$$

where  $(c_{1d}, c_{1q})$  are positive constants of synthesis.

As  $x_{2d}/C_f$  and  $x_{2q}/C_f$  are not the actual control inputs, a new vector error, denoted  $E_2$ , is introduced:

$$E_2 = \begin{pmatrix} e_{2d} \\ e_{2q} \end{pmatrix} = \begin{pmatrix} x_{2d}/C_f - \sigma_d \\ x_{2q}/C_f - \sigma_q \end{pmatrix} \quad (15)$$

Then, equation (11) becomes, using (14) and (15):

$$\dot{E}_1 = \begin{pmatrix} \dot{e}_{1d} \\ \dot{e}_{1q} \end{pmatrix} = \begin{pmatrix} -c_{1d}e_{1d} + e_{2d} - \tilde{\delta}x_{1d} \\ -c_{1q}e_{1q} + e_{2q} - \tilde{\delta}x_{1q} \end{pmatrix} \quad (16)$$

Also, the derivative of Lyapunov function (13) becomes:

$$\begin{aligned} \dot{W}_1 = & -c_{1d}e_{1d}^2 + e_{1d}e_{2d} - c_{1q}e_{1q}^2 + e_{1q}e_{2q} \\ & - \frac{1}{\gamma} \tilde{\delta} \left( \dot{\tilde{\delta}} + \gamma(x_{1d}e_{1d} + x_{1q}e_{1q}) \right) \end{aligned} \quad (17)$$

**Step2:** Stabilization of the subsystem

$$(e_{1d}, e_{1q}, e_{2d}, e_{2q}, \tilde{\delta})$$

Time-derivation of  $E_2$  gives, using (14) and (2b):

$$\dot{E}_2 = \begin{pmatrix} \dot{e}_{2d} \\ \dot{e}_{2q} \end{pmatrix} = \begin{pmatrix} \frac{1}{C_f} \left( \omega x_{2q} + \frac{x_{dc}}{2L_f} u_d - \frac{1}{L_f} x_{1d} \right) - \dot{\sigma}_d \\ \frac{1}{C_f} \left( -\omega x_{2d} + \frac{x_{dc}}{2L_f} u_q - \frac{1}{L_f} x_{1q} \right) - \dot{\sigma}_q \end{pmatrix} \quad (18)$$

Derivatives of stabilizing functions can be written in the following form:  $\dot{\sigma}_d = \alpha_d + \beta_d \tilde{\delta}$  and  $\dot{\sigma}_q = \alpha_q + \beta_q \tilde{\delta}$

The actual control variables, namely,  $u_d$  and  $u_q$  appears for the first time (18). Let us consider the Lyapunov function.

$$W_2 = W_1 + \frac{1}{2} e_{2d}^2 + \frac{1}{2} e_{2q}^2 \quad (19)$$

Using (17), the time-derivative of  $W_2$  can be rewritten as:

$$\begin{aligned} \dot{W}_2 = & -c_{1d}e_{1d}^2 - c_{1q}e_{1q}^2 + e_{2d}(e_{1d} + \dot{e}_{2d}) \\ & + e_{2q}(e_{1q} + \dot{e}_{2q}) - \frac{1}{\gamma} \tilde{\delta} \left( \dot{\tilde{\delta}} + \gamma(x_{1d}e_{1d} + x_{1q}e_{1q}) \right) \end{aligned} \quad (20)$$

This shows that, for the  $(e_{1d}, e_{1q}, e_{2d}, e_{2q}, \tilde{\delta})$ -system to be globally asymptotically stable, it is sufficient to choose the control  $u_d$ ,  $u_q$  and  $\dot{\tilde{\delta}}$  so that  $\dot{W}_2 = -c_{1d}e_{1d}^2 - c_{1q}e_{1q}^2 - c_{2d}e_{2d}^2 - c_{2q}e_{2q}^2$  which, due to (20), amounts to ensuring that:

$$\dot{E}_2 = \begin{pmatrix} \dot{e}_{2d} \\ \dot{e}_{2q} \end{pmatrix} = \begin{pmatrix} -c_{2d}e_{2d} - e_{1d} - \tilde{\delta}\beta_d \\ -c_{2q}e_{2q} - e_{1q} - \tilde{\delta}\beta_q \end{pmatrix} \quad (21)$$

Comparing (18) and (21) yields the following backstepping control laws  $u_d$  and  $u_q$ :

$$u_d = \left[ (2L_f C_f) / x_{dc} \right] \left[ -c_{2d}e_{2d} - e_{1d} - \omega x_{2q}/C_f + x_{1d}/L_f C_f + \alpha_d \right] \quad (22)$$

$$u_q = \left[ (2L_f C_f) / x_{dc} \right] \left[ -c_{2q}e_{2q} - e_{1q} + \omega x_{2d}/C_f + x_{1q}/L_f C_f + \alpha_q \right] \quad (23)$$

and adaptation law is:

$$\dot{\tilde{\delta}} = -\dot{\delta} = \gamma(x_{1d}e_{1d} + x_{1q}e_{1q} + \beta_d e_{2d} + \beta_q e_{2q}) \quad (24)$$

### 3.3 DC voltage outer loop design

The aim of the outer loop is to generate a tuning law for the signal  $\beta$  so that the output voltage  $x_{dc}$  is steered to a given reference value  $x_{dc}^*$ . This is the subject of the following proposition.

**Proposition:** Consider the single-phase to three-phase described by (1, 2 and 3) augmented with the inner control laws defined by (8), (22) and (23), one has the following:

The squared-voltage  $y = (x_{dc})^2$  varies, in response to the tuning ratio  $\beta$ , according to the following first-order time-varying linear equation:

$$\dot{y} = f(\beta) + p(t) + q(x_{dq}) \quad (25)$$

with

$$f(\beta) = k_0 \beta (1 - r_s \beta) \quad ; \quad p(t) = -f(\beta) \cos(2\omega t)$$

$$q(x_{dq}) = -\frac{2}{C} (x_{1d} x_{2d} + x_{1q} x_{2q} + \alpha_d x_{2d} + \alpha_q x_{2q})$$

$$\text{where} \quad k_0 = E^2 / C$$

**Proof:** it is identical to a similar result in [6]

The current problem is to design a suitable control law so that the square of the voltage  $y = (x_{dc})^2$  follows a reference signal given  $y^* = (x_{dc}^*)^2$ . As the term disruptive  $p(t)$  in (25), is periodic with zero mean and a control law PI with compensation for non-linearity  $q(x_{dq})$ , should suffice:

$$f(\beta) = c_3 e_3 + c_4 e_4 - q(x_{dq}) + y^* \quad (26)$$

$$\text{with} \quad e_3 = y^* - y \quad ; \quad e_4 = \int_0^t e_3 d\tau$$

Substituting equation (25) in (26), we obtain the equations errors  $e_3$  and  $e_4$ .

$$\begin{cases} \dot{e}_3 = -c_3 e_3 - c_4 e_4 - p(t) \\ \dot{e}_4 = e_3 \end{cases} \quad (27)$$

At this point, the regulator parameters  $(c_3, c_4)$  are any positive real constants. The actual control signal  $\beta$  can be easily obtained from (26) using the fact that  $f^{-1}(\cdot)$  exists.

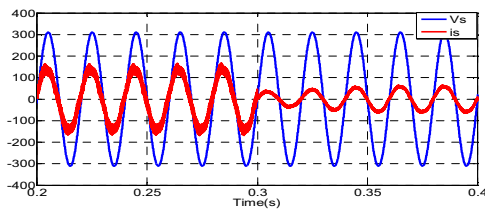
### 4 Numerical Simulations

The performances of proposed controllers are validated by simulation in MATLAB/SIMULINK environment. The parameters of the controlled system are given in the table 2. The main voltage is fixed at its nominal value  $v_s(t) = E \sin(\omega t)$ . Figures 2 to 5 show the simulation results of uninterrupted power system based on the single-phase to three-phase under the effect of a load change when the reference DC bus voltage is set at 1600V. The variable load R is periodic with period 0.6 s alternates between 10 and 20 in each half period.

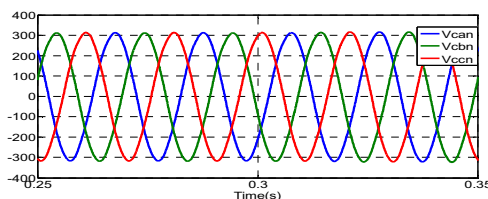
**Table 2.** System parameters controlled.

Parameters	Symbol	Values
Network	$E, f$	$220\sqrt{2} \text{ V}, 50\text{Hz}$
Rectifier	$L_s$	$2\text{mH}$
	$r_s$	$30\text{m}\Omega$
Dc Bus	$C$	$47 \text{ mF}$
Three-phase inverter	$L_f$	$100\text{mH}$
	$C_f$	$100\mu\text{F}$
PFC Regulator	$c_i$	$2 \times 10^3$
Three phase system Regulator	$c_{1d} = c_{1q}$	1000
	$c_{2d} = c_{2q}$	$10^4$
	$\gamma$	$10^{-6}$
DC voltage Regulator	$c_3$	$2 \times 10^{-5}$
	$c_4$	$6 \times 10^{-4}$

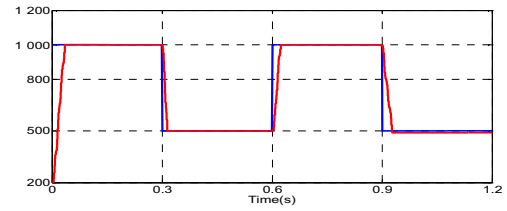
In Figure 2, we see that the current  $i_s$  and the input voltage  $v_s$  are sinusoidal and in phase with the current amplitude change inversely proportional to the change of the load. This shows that the correction of the power factor is well established. Figure 3 shows the evolution of the output phase voltages  $v_{Can}$ ,  $v_{Cbn}$  and  $v_{Ccn}$  of the three phase inverter which is a three-phase system that provides balance even if the load changes. This is because the estimated  $\hat{\delta}$  converges rapidly to its true value (Figure 4). Finally, Figure 5 shows that the DC bus voltage  $x_{dc}$  perfectly follows (in average) its reference.



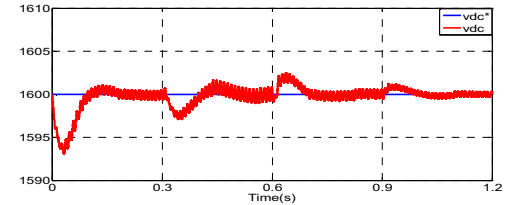
**Fig. 2.** Input voltage  $v_s$  and input current  $i_s$



**Fig. 3.** Phase output voltages  $v_{Can}$ ,  $v_{Cbn}$  and  $v_{Ccn}$



**Fig. 4.** Estimated parameter  $\hat{\delta}$  (red) in the presence of  $\delta$  (blue)



**Fig. 5.** DC bus voltage  $x_{dc}$  and reference  $x_{dc}^*$

### Conclusion

In this paper, an adaptive nonlinear controller is proposed for the single-phase to three-phase UPS System used in power systems without interruption. It has been formally established that the obtained controller meets its objectives such as: i) unity input power factor PFC feature is enabled, ii) high-quality sinusoidal output voltages, even with a unknown resistive load, iii) regulation of the DC bus voltage, and iv) excellent transient characteristics and stability.

### References

- [1] F. Giri, A. Abouloifa, I. Lachkar, F.Z. Chaoui, Nonlinear Control of PWM AC/DC Boost Rectifiers: Theoretical Analysis of Closed-Loop Performances, 17th Proceedings of the IFAC World Congress, Seoul, Korea, (2008).
- [2] J.Y. Choi, J. Farrell, Observer-based Backstepping Control Using Online Approximation, American Control Conference, 5, 3646-3650, (2000).
- [3] R. Ghosh, G. Narayanan, A Simple Analog Controller for Single-Phase Half-Bridge Rectifier and its Application to Transformerless UPS, IEEE IISC, (2005).
- [4] S-El-M. Ardjoun, M. Abid, A-G. Aissaoui, A. Naceri, A robust fuzzy sliding mode control applied to the double fed induction machine, International Journal Of Circuits, Systems And Signal Processing 4, 5, pp. 315-321, NAUN, USA, (2011).
- [5] S. Chattopadhyay, V. Ramanaryanan, A single-reset-integrator-based implementation of lince-current-shapping controller for high-power-factor operation of flyback rectifier, IEEE Trans. on industry application 38, 490-499, March-April (2002).
- [6] M. Kissaoui, A. Abouloifa, F. Giri, F.Z. Chaoui, Y. Abouelmahjoub, Nonlinear Control of New Single-Phase to Three-Phase Hybrid UPS System, International Conference on Control, Engineering & Information Technology (CEIT'14), 6, 109-117 (2014).